

Shock accelerated two-dimensional interface

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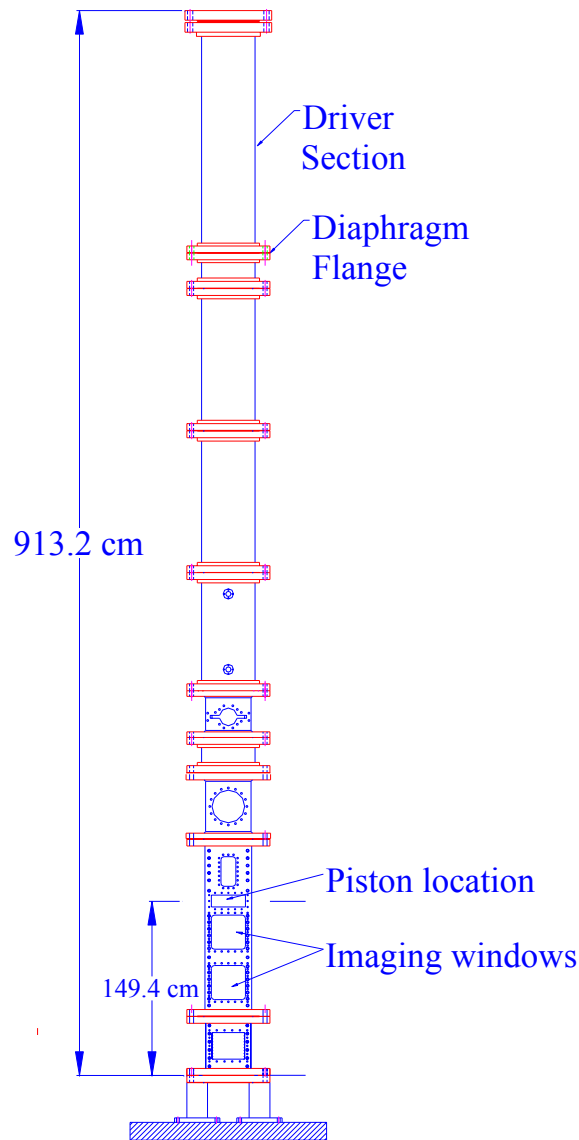
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the Physics of Compressible Turbulent Mixing

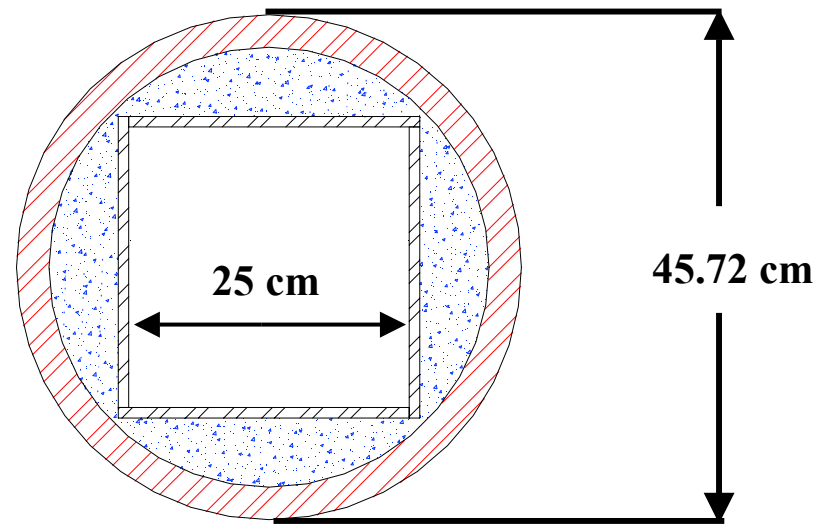
Paris, France

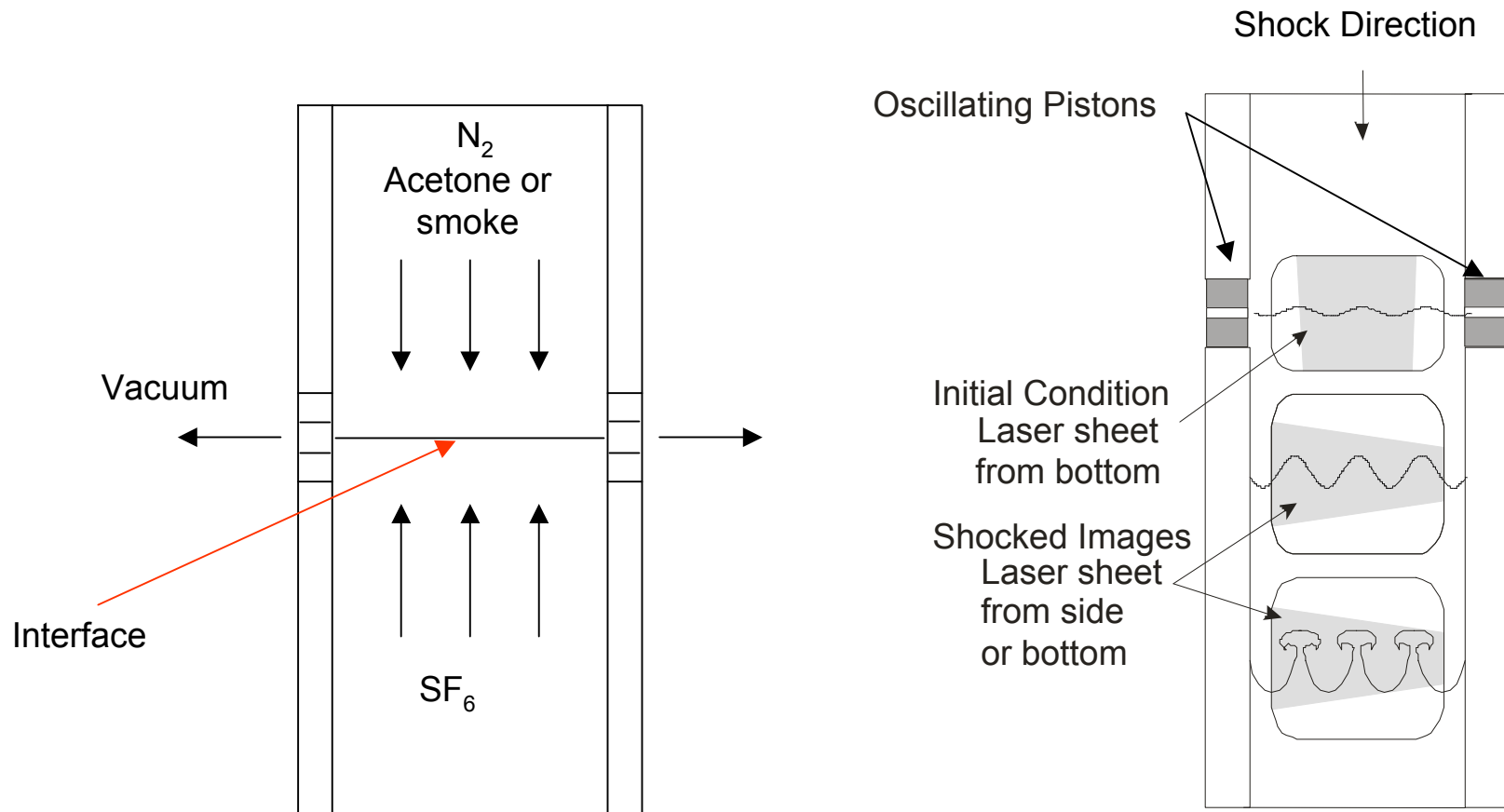
Work supported by US DOE under Grant # DE-FG52-03NA00061

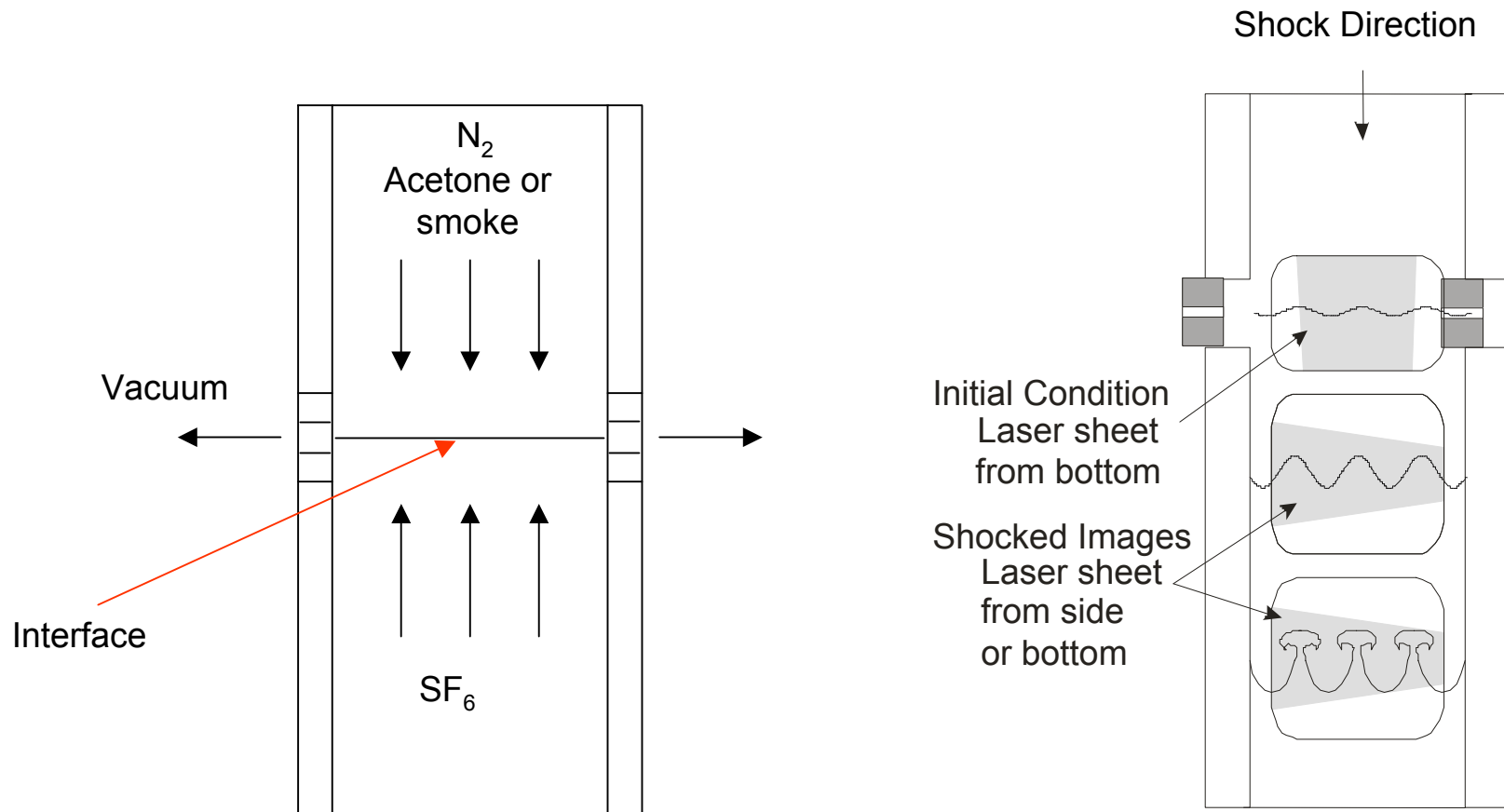


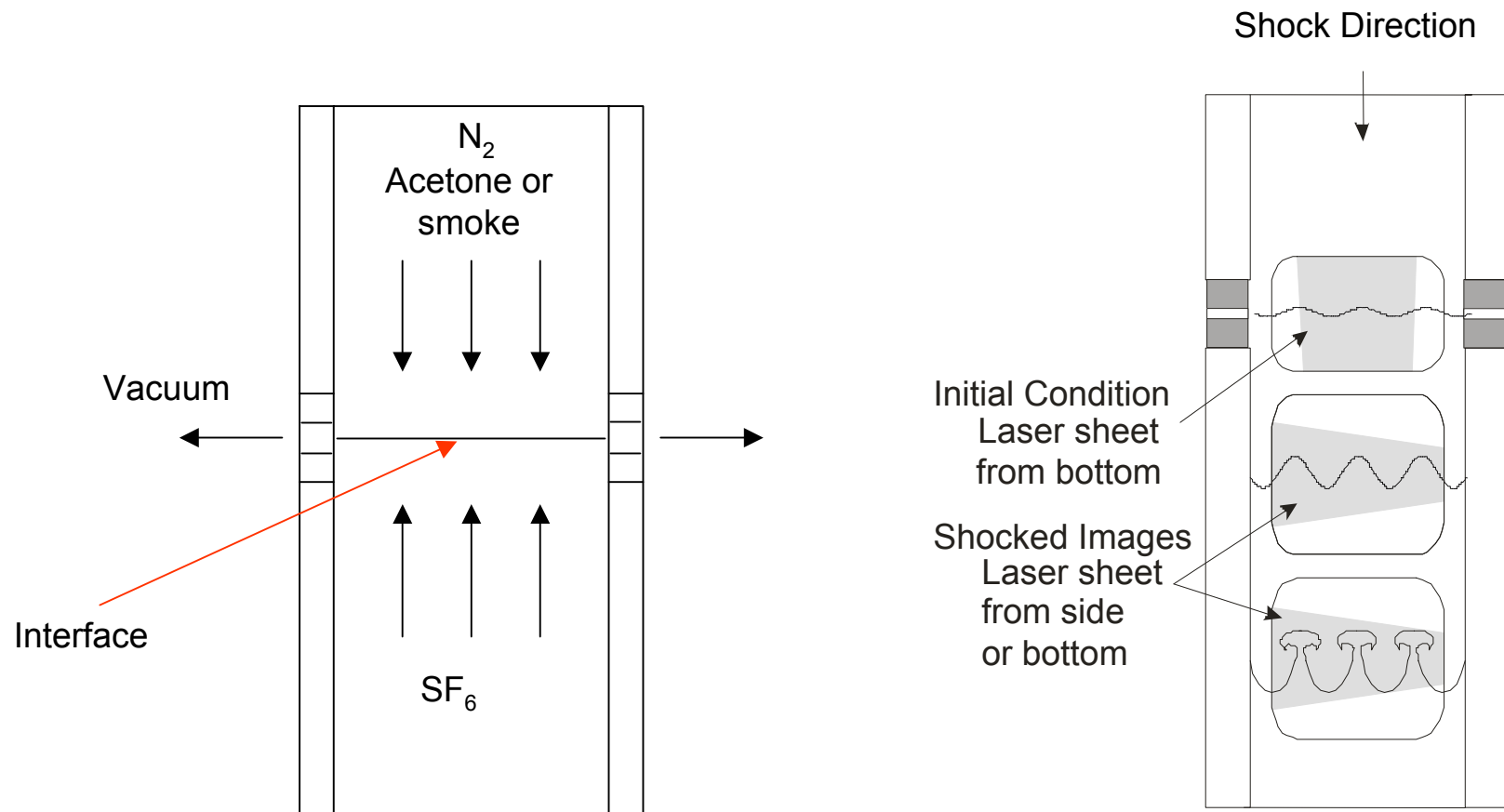


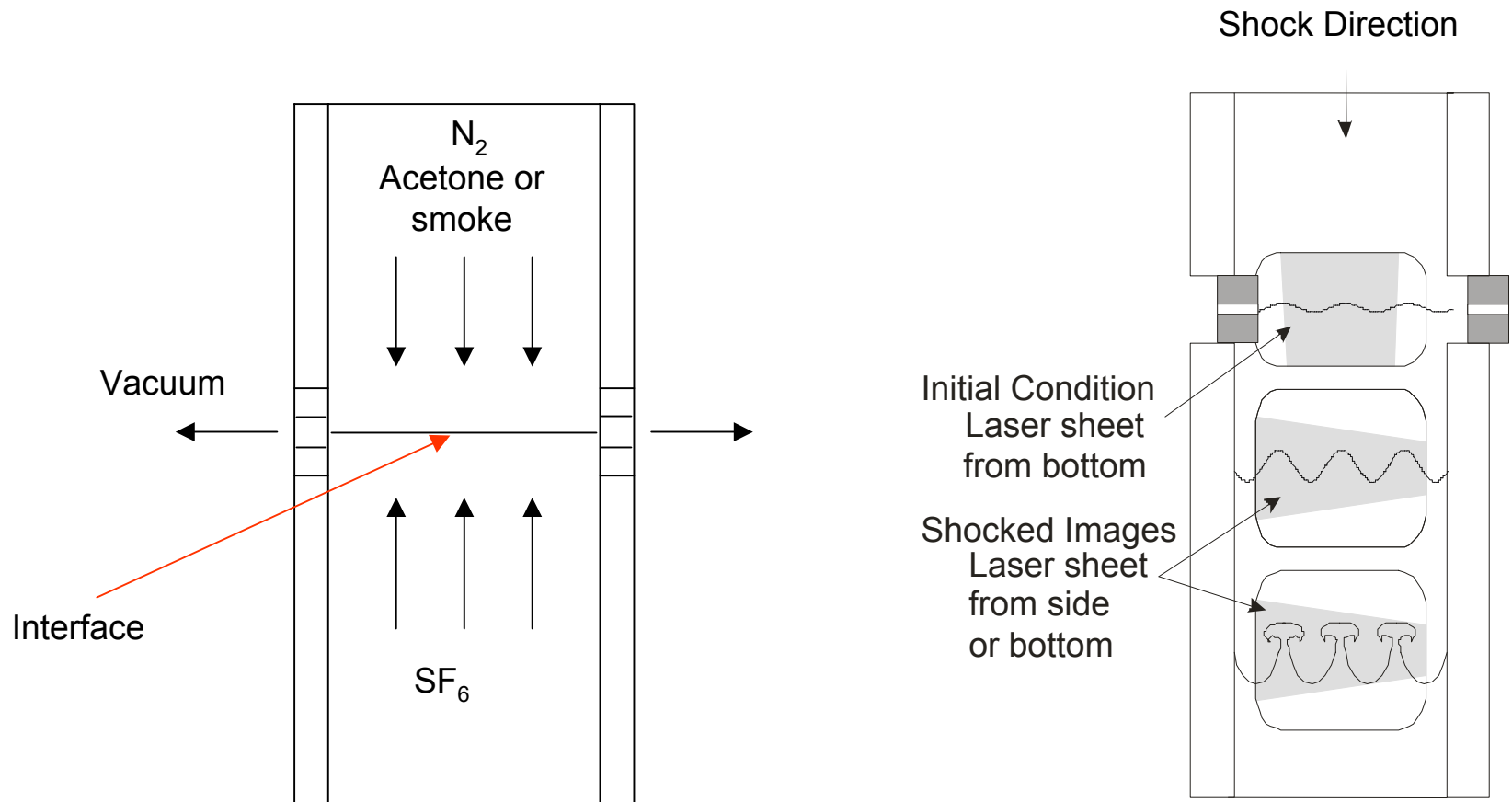
- Vertical
- Large internal cross-section (25 cm square)
- Total length 9.2 m, driver length 2 m
- Pressure load capability: 20 MPa
- Modular driven section

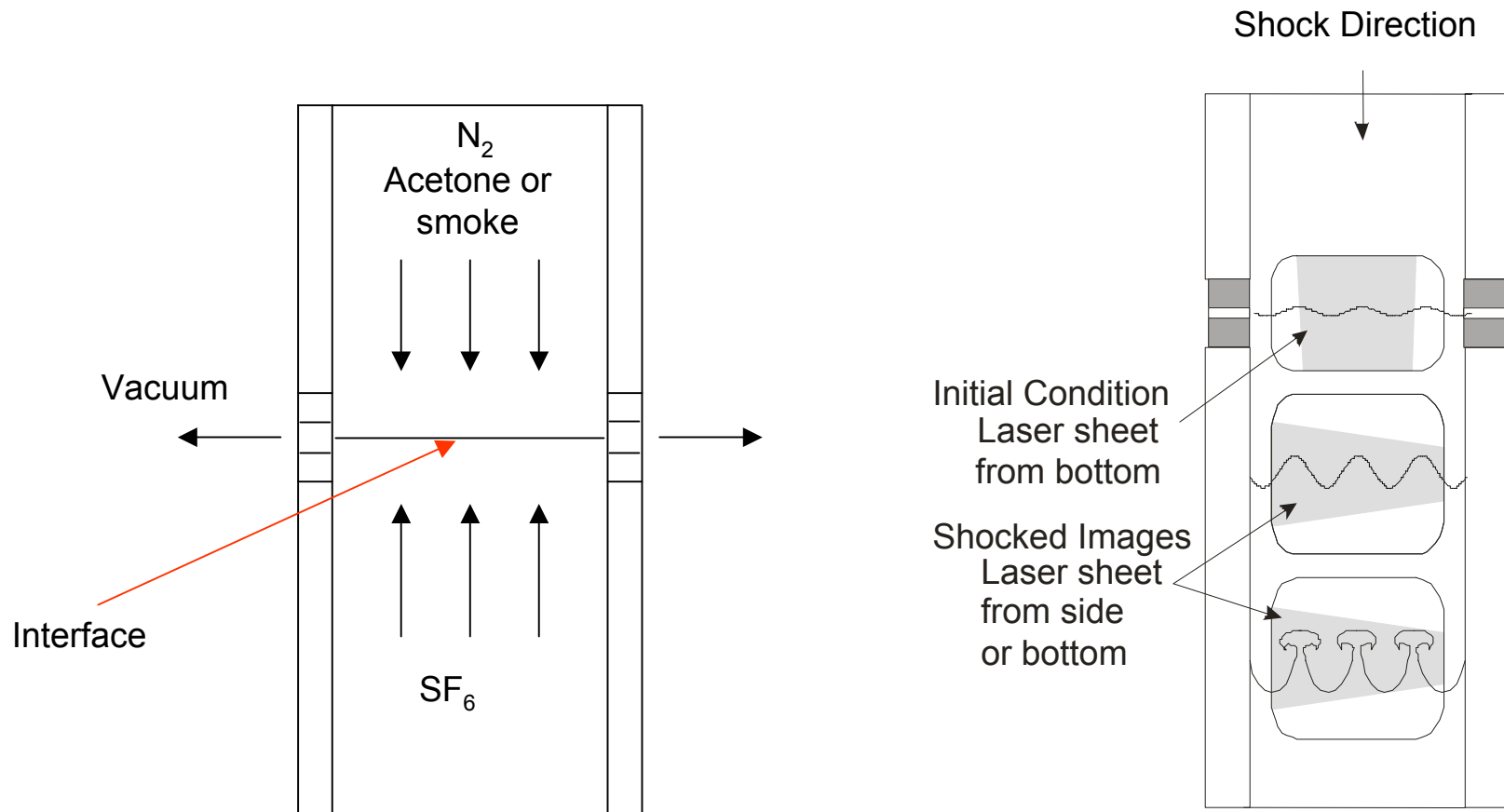










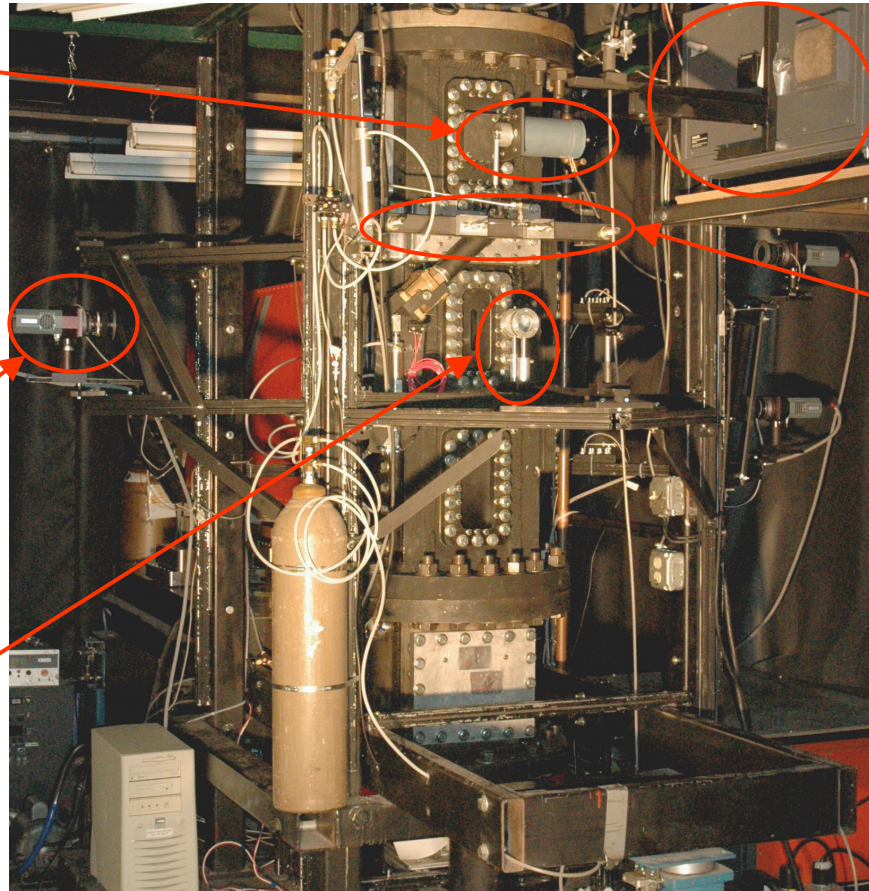


TEST SECTION

Stepper motor

1024 x 1024
CCD Array

Laser sheet
forming optics

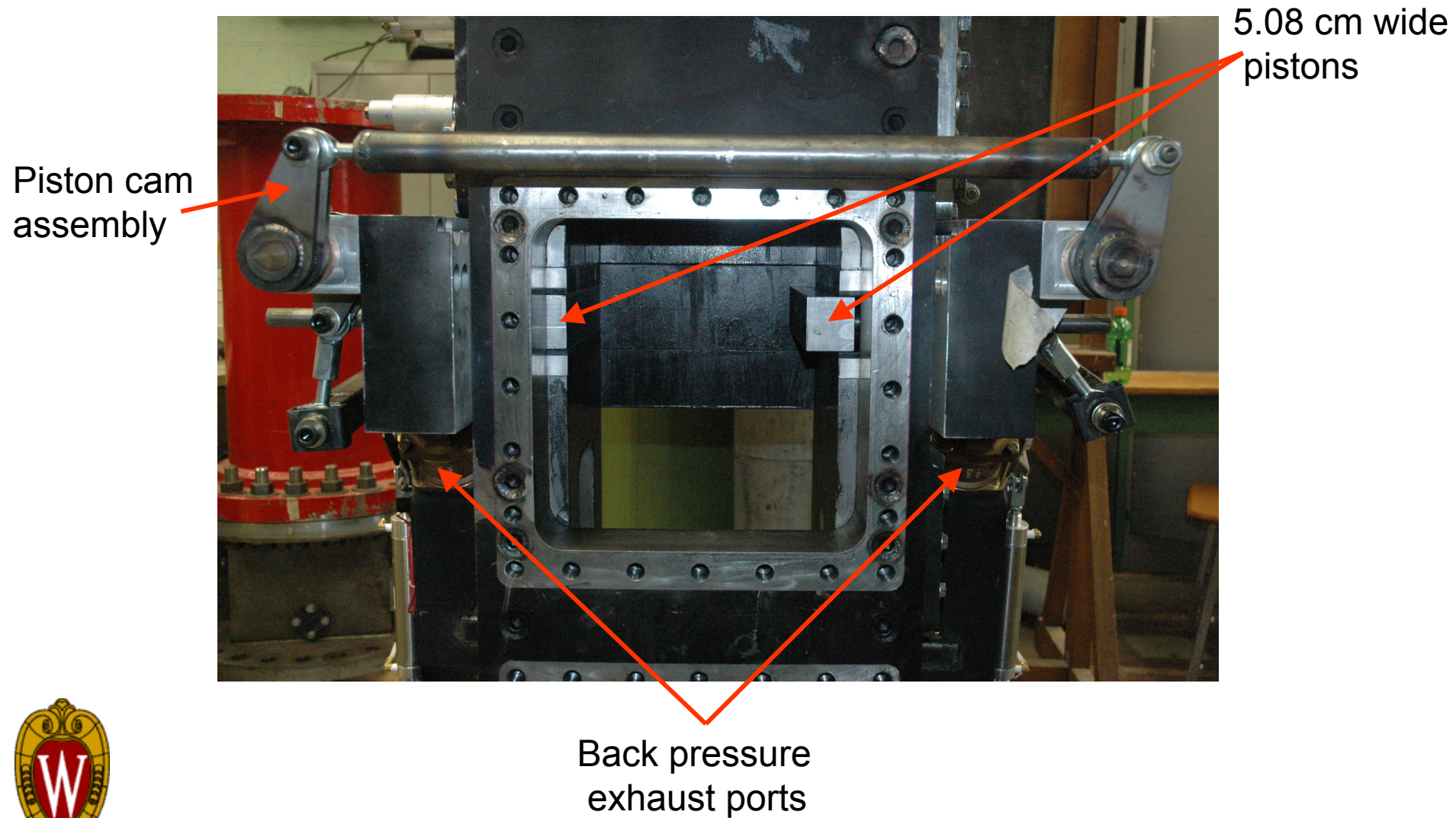


Excimer Laser
 $\lambda = 248 \text{ nm}$
 $E \approx 550 \text{ mJ / pulse}$

Piston



PISTON ASSEMBLY

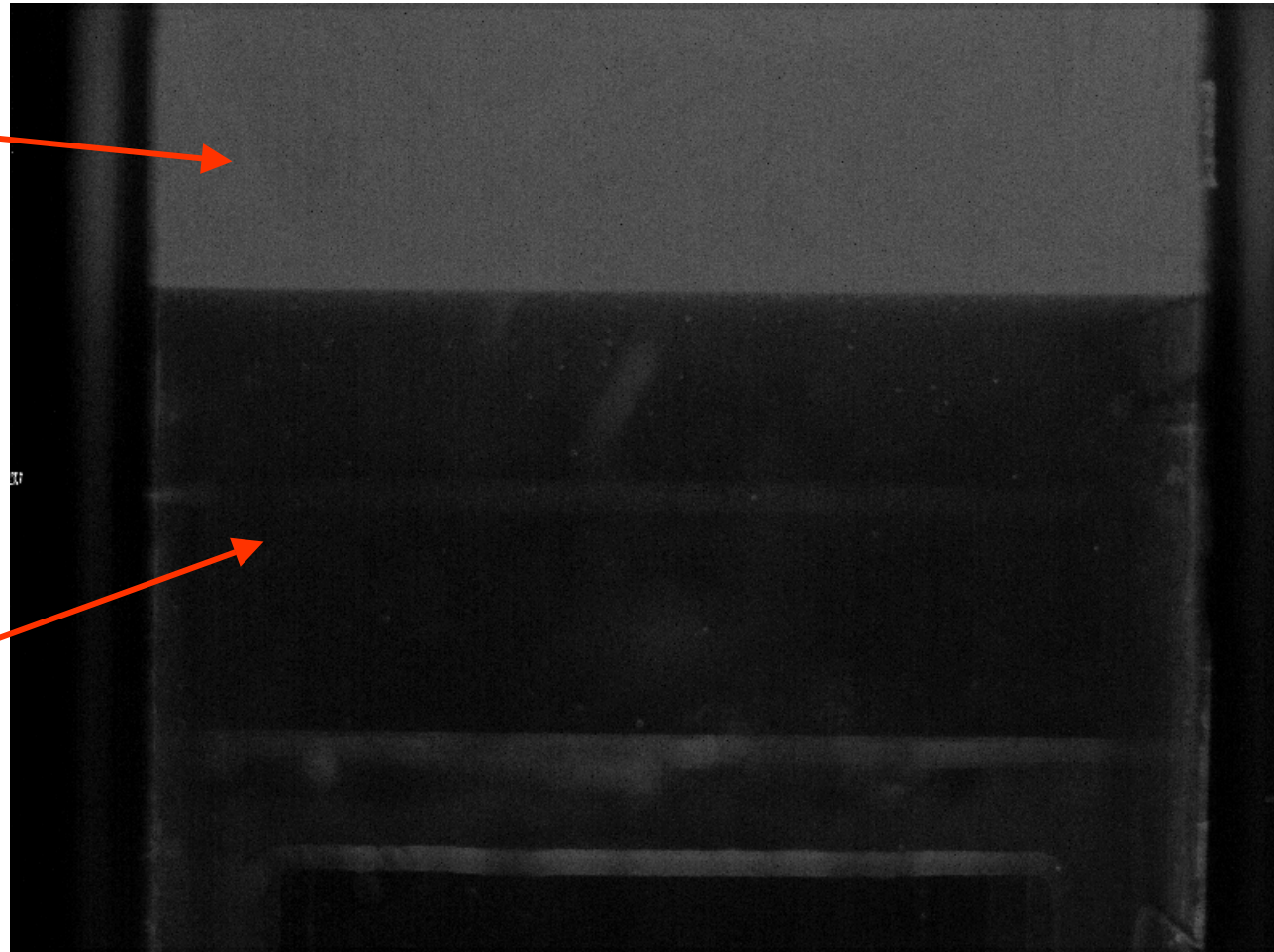


	A	B	C
Light gas	N ₂	N ₂	N ₂
Heavy gas	SF ₆	SF ₆	SF ₆
Tracer	acetone	acetone	smoke
<i>M</i> (initial)	1.26	1.26	2.05
<i>A</i> (pre)	0.643	0.643	0.678
<i>A</i> (post)	0.672	0.672	0.771
η (pre)	0.78 - 0.81 cm	0.52 - 0.82 cm	0.64 - 0.97 cm
η (post)	0.57 - 0.58 cm	0.39 - 0.58 cm	0.37 - 0.57 cm
λ	9.4 cm	17.9 cm	16.8 cm
<i>k</i>	0.670 cm ⁻¹	0.351 cm ⁻¹	0.374 cm ⁻¹



N_2 seeded with smoke

SF_6

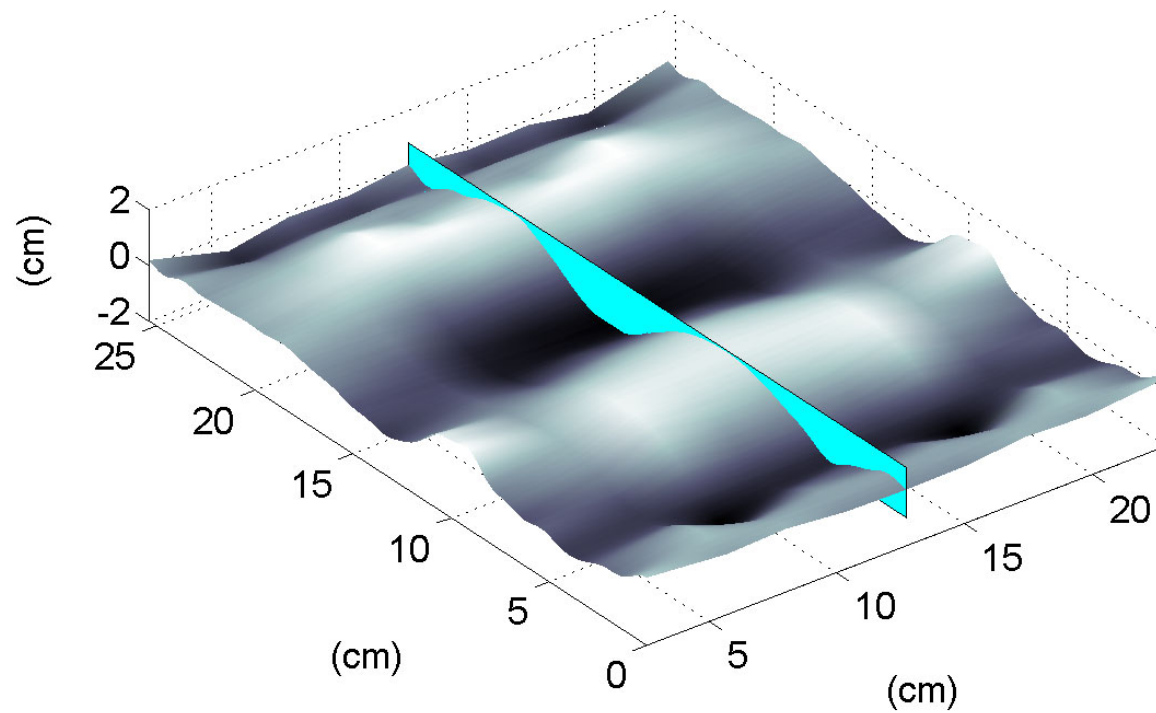


Pistons oscillate at 2.1 Hz (0.476 second period),
for 3 revolutions.

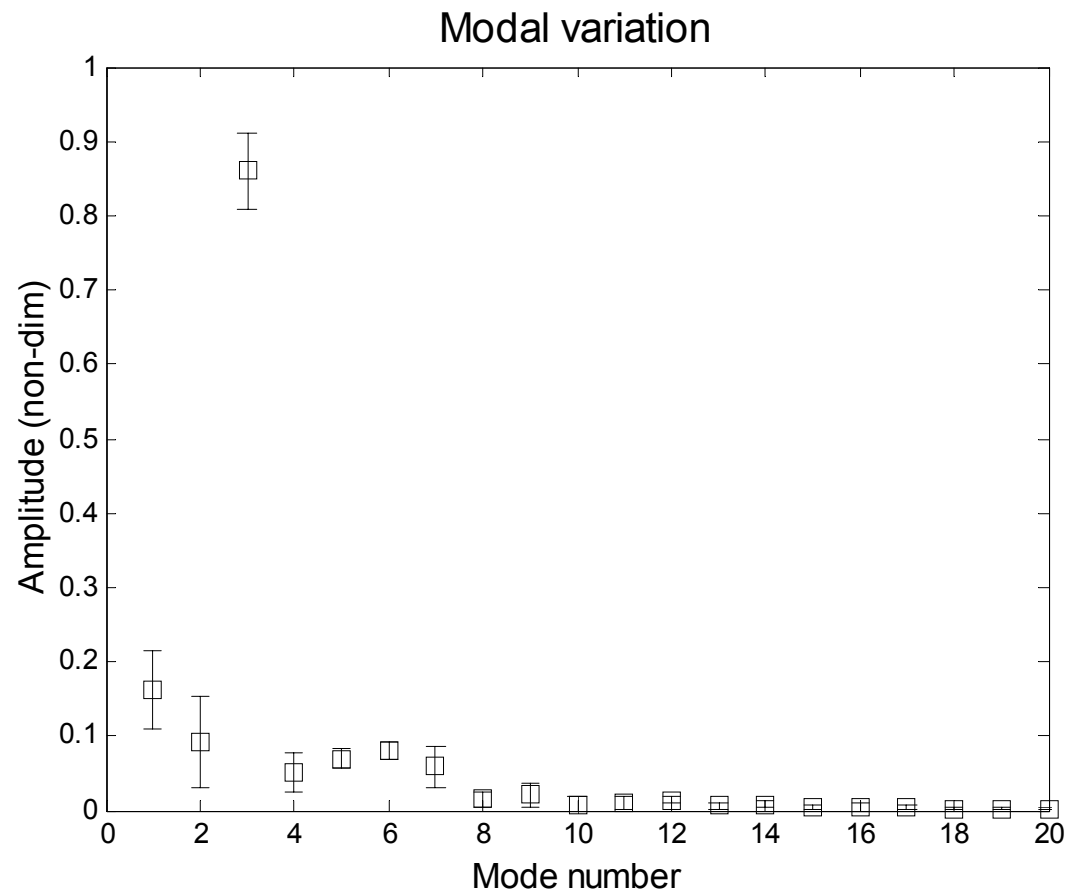


Distone oscillating at 1.0 Hz

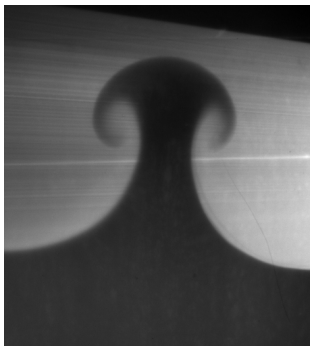
Initial Condition 3D Reconstruction



Initial condition modal content (6 test sample)



- a) Raw image
- b) Mapped image
- c) Mapped image corrected using Beer's Law
- d) Re-mapped corrected image



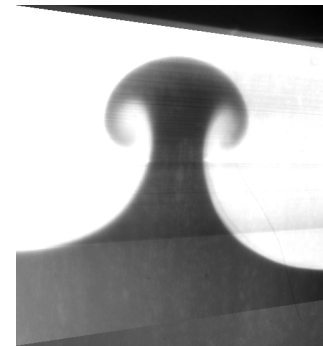
a



b



c



d



2D hydrodynamic code – Raptor (LLNL)

- a) solves the multi-fluid compressible Euler equations, with an ideal gas law equation of state
- b) a shock-capturing scheme and higher-order Godunov solver is used to handle shock propagation accurately and suppress spurious oscillations
- c) fixed (Eulerian) grid in 2-D Cartesian geometry, 512 grid points in the transverse dimension
- d) two levels of adaptive mesh refinement (AMR) on the fluid interface
- e) initial condition is characterized using a Fourier transform
- f) the interface is smeared vertically using a hyperbolic tangent distribution fitted to the diffusion characteristics of the experimental interface



Following Jacobs & Krivets, Physics of Fluids 17, 034105 (2005)

$$\text{Non – dimensional amplitude} = ka - ka_0 = \eta$$

where k is the wave number, a_0 is the initial amplitude and a is the amplitude

$$\text{Non – dimensional time} = k\dot{a}_0 t = \tau$$

where \dot{a}_0 is the post shock growth rate, and t is time

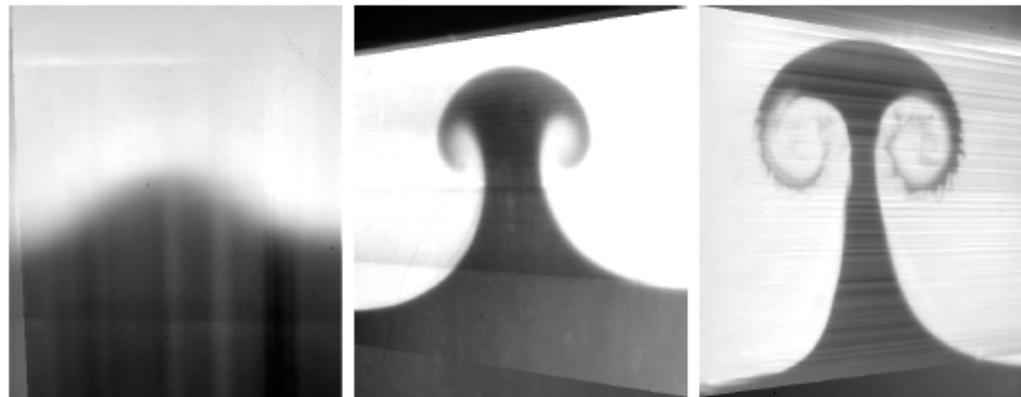
In the analysis presented, the approximation $\dot{a}_0 \approx ka_0 A \Delta V$ is utilized,

where A is the post shock Atwood number and ΔV is the velocity change of the interface due to impulsive acceleration of the shock wave

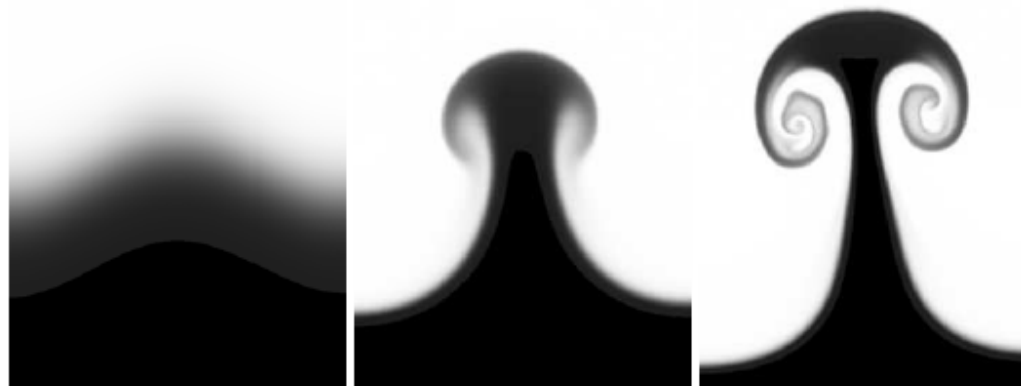


$M = 1.26$, 2.6 Hz driving frequency, $\lambda = 90$ mm, $a_{0-} = 6.11$ mm

Experiment



RAPTOR

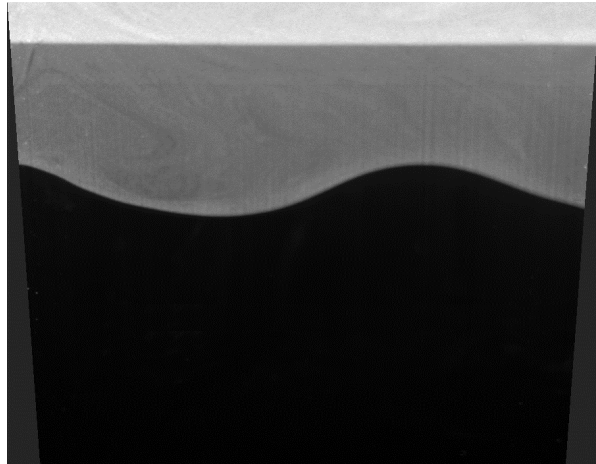


$\tau = 0.00$

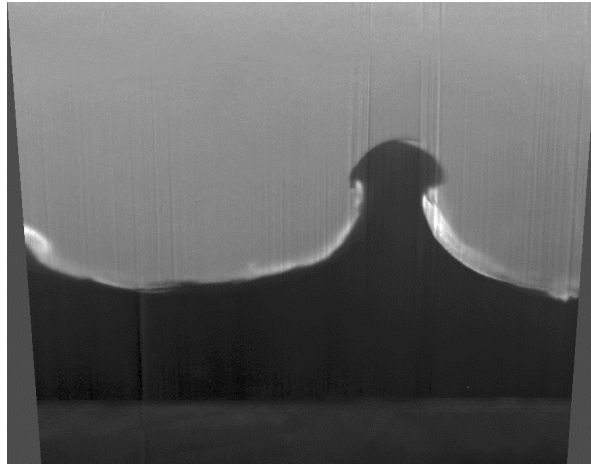
$\tau = 4.66$

$\tau = 8.79$

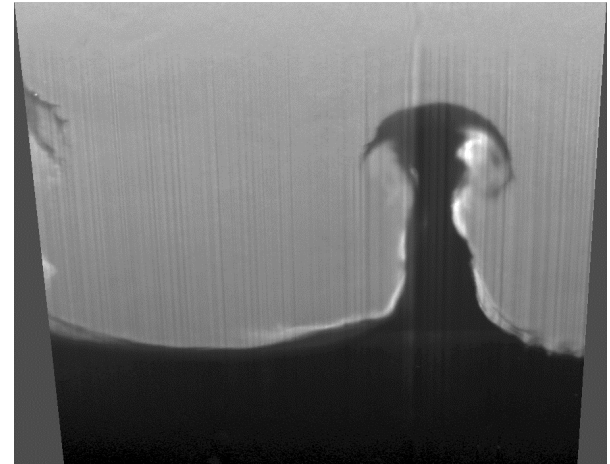




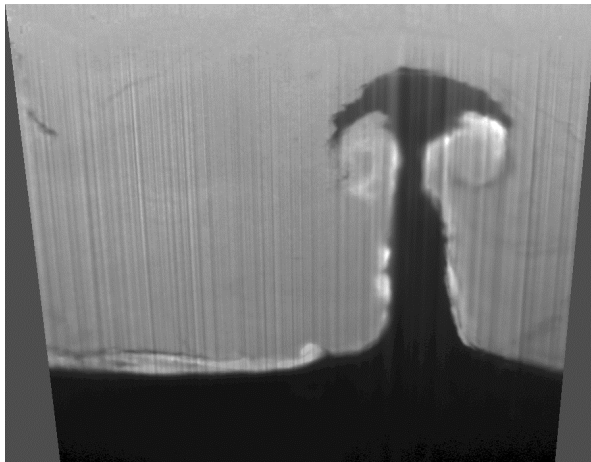
$\tau = 0.00$



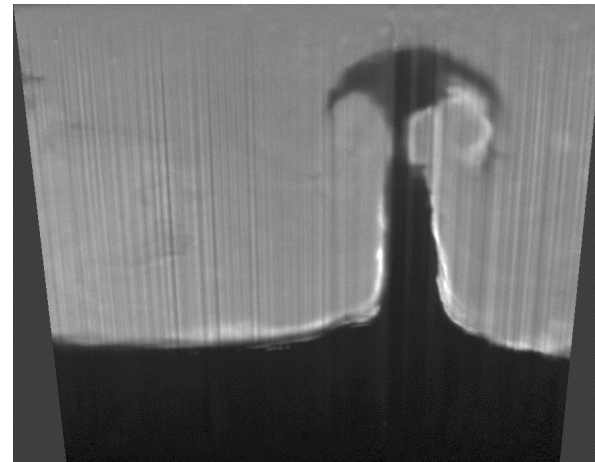
$\tau = 1.54$



$\tau = 3.29$



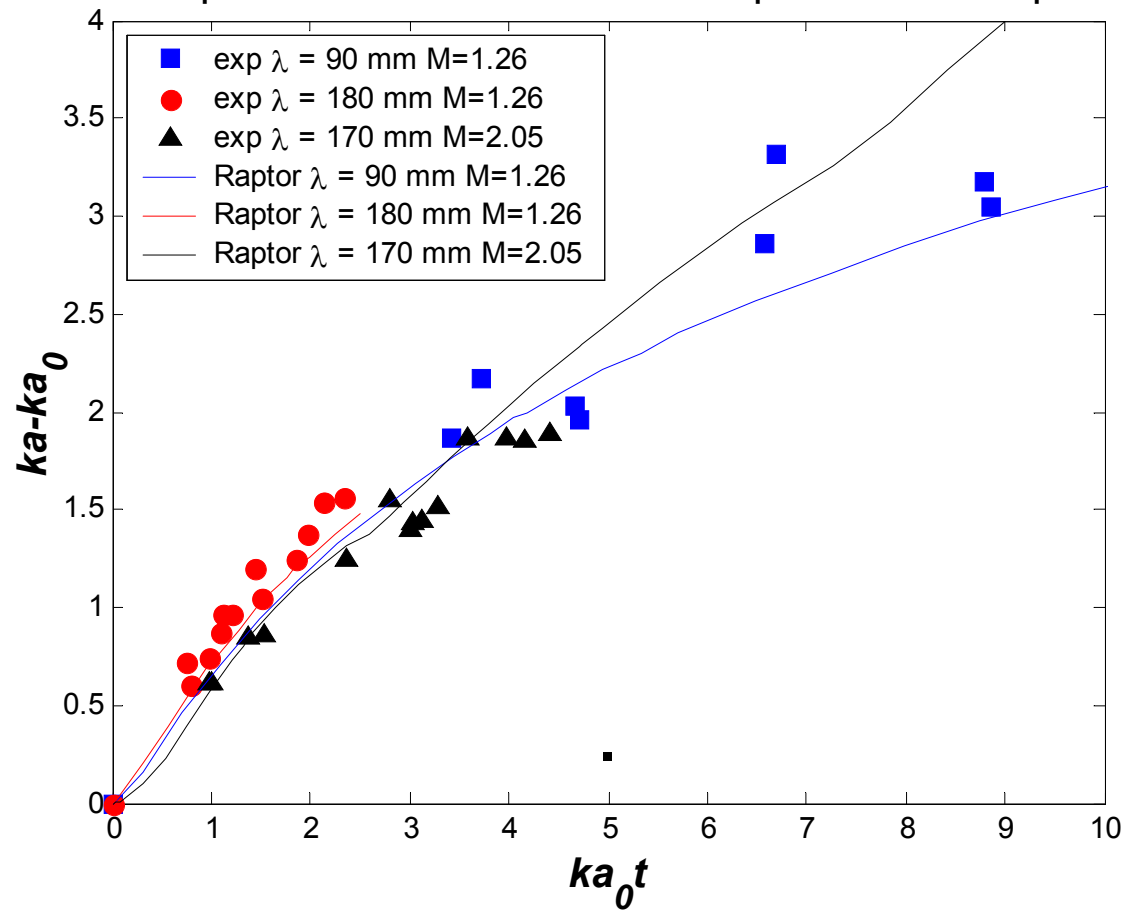
$\tau = 3.98$



$\tau = 4.16$



Comparison of dimensionless amplitude with Raptor



1) Sadot et al., Phy Rev Lett Vol. 80 Number 8 (1998)

$$a(t) = \left[\frac{\dot{a}_0}{(4E - D^2)^{\frac{1}{2}}} \left(2 - \frac{BD}{E} \right) \right] \times \tan^{-1} \left[\frac{2Et + D}{(4E - D^2)^{\frac{1}{2}}} \right] + \frac{\dot{a}_0 B}{2E} \ln(1 + Dt + Et^2) + K$$

2) Mikaelian, Physical Review E 67, 026319 (2003)

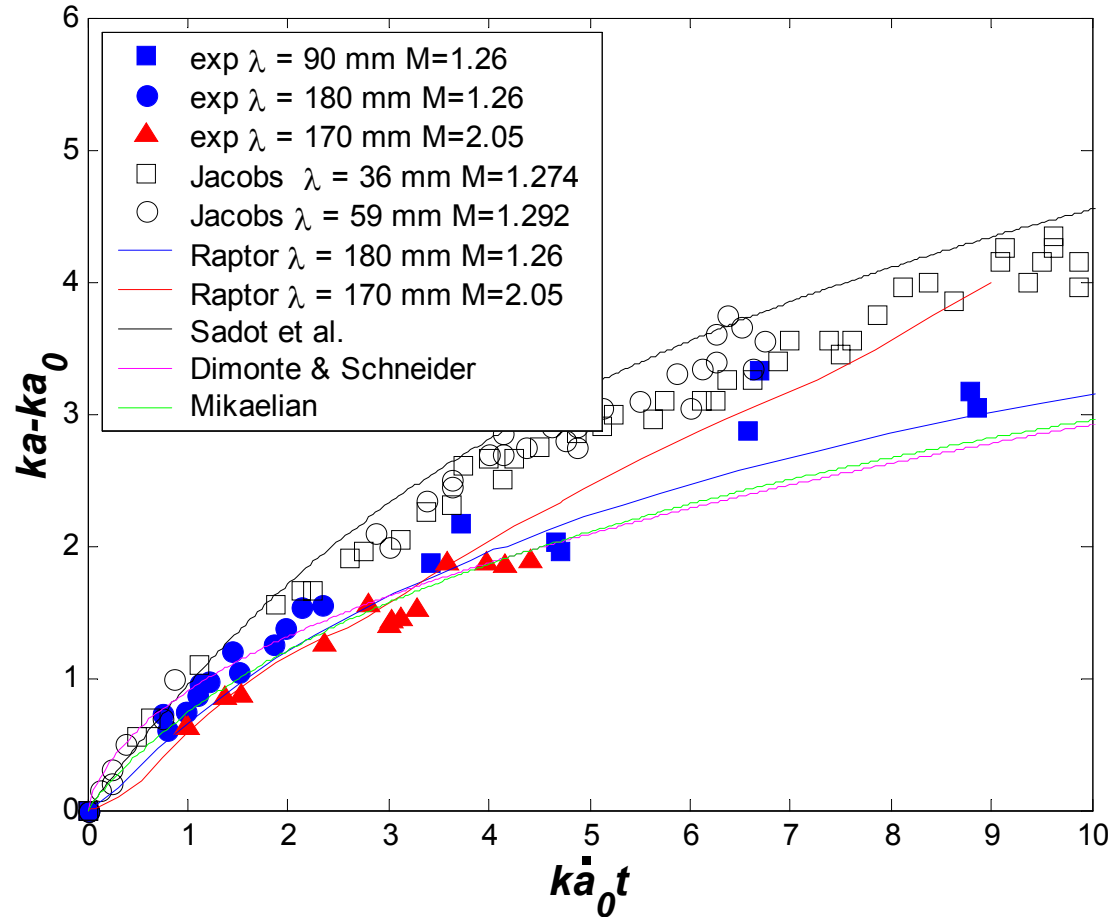
$$a(t) = a_0 + \frac{3 + A}{3(1 + A)k} \ln \left(1 + 3 \dot{a}_0 kt \frac{1 + A}{3 + A} \right)$$

3) Dimonte & Schneider, Physics of Fluids Vol. 12 Number 2 (2000)

$$a(t) = a_0 \tau_i^{\theta_i} \quad \text{where} \quad \tau_i = \frac{V_{i0}(t - t_0)}{\theta_i a_0} + 1$$



Comparison of dimensionless amplitude with several models



* Jacobs data taken from Figure 7 of J.W. Jacobs & V.V. Krivets
Physics of Fluids 17, 034105 (2005) paper.



- 1) Oscillating piston technique suitable for setup of 2D initial conditions
- 2) Same geometrical features as in low M experiments at much earlier dimensionless times
- 3) Satisfactory agreement between the experiment and Raptor at $M = 1.26$ and $M = 2.05$ at early times (but intermediate M expts. suggest saturation while code doesn't)
- 4) Satisfactory agreement with Mikaelian and Dimonte & Schneider models at $M = 1.26$ and $M = 2.05$ (but intermediate M expts. suggest saturation while models don't)
- 5) Is current normalization missing compressibility effects? (more in bubble expts. and corresponding calculations)

