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Shield for a CTR Magnet**

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A quantitative study of the shield for fusion reactors operating on the D-T cycle and utilizing a magnetic confinement scheme was carried out [1]. A summary of some of the results follows.

The shield is required to perform three major functions: 1 - reduce the nuclear heating of the cryogenic coils to a permissible level; 2 - reduce the radiation damage to the superinsulation, for a 20 yr. lifetime; 3 - keep the radiation to the magnet to the minimum allowed by a) the tolerable increase in the resistivity of the copper stabilizer and b) the radiation damage to the superconductor. The energy attenuation required by the refrigeration system can be determined by a compromise between its operating and capital cost, the shield cost, and the increase in the magnet cost if the shield thickness is increased. However, an increase in the resistivity of the stabilizer and radiation damage to the superconductor cannot be compromised beyond the tolerable level. Fortunately, the optimum shield thickness from a cost standpoint results in acceptable levels of damage to the superinsulation and magnet stabilizer, as can be seen from figure 1 and results below.

A study of the effectiveness of various compositions in the shield region showed that a mixture of stainless steel and boron carbide results in a minimum shield thickness for the required total energy attenuation. The total energy attenuation varies exponentially with the shield thickness. The attenuation coefficients for the respective shield compositions were a -  $0.1445 \text{ cm}^{-1}$  for 70% SS plus 30%  $\text{B}_4\text{C}$ , b -  $0.1113 \text{ cm}^{-1}$  for 70% Pb plus 30%  $\text{B}_4\text{C}$ , c -  $0.1283 \text{ cm}^{-1}$  for 35% SS plus 35% Pb plus 30%  $\text{B}_4\text{C}$ ,

and  $d = 0.0902 \text{ cm}^{-1}$  for 100% SS. The blanket was the same for all cases; viz., 50 cm lithium and 20 cm SS.

Increasing the thickness of the shield increases both shield and magnet costs, but lowers the refrigeration power requirements. To minimize the total cost with respect to the shield thickness, consider a toroidal reactor and the following equations.

$$C_M = a_m r_m^m, \quad r_m = r_b + t_s \quad (1)$$

$$C_S = \pi(t_s^2 + 2r_b t_s) \cdot a_s \quad (2)$$

$$C_R = a_r e^{-0.6\mu_s t_s} \quad (3-a)$$

$$a_r = 6000(2\pi r_w W_n e^{-\mu_b t_b})^{0.6} \quad (3-b)$$

where  $C_M$ ,  $C_S$ ,  $C_R$  are magnet, shield, and refrigeration costs, respectively, per unit length in the toroidal direction;  $r_w$  and  $r_b$  are the inner and outer blanket radii;  $t_s$  is shield thickness and is the parameter to be optimized;  $W_n$  is neutron wall loading;  $\mu_b$  and  $\mu_s$  are energy attenuation coefficients in the blanket and shield. We assume that the magnet cost increases with its inner radius to the power  $m$  and the refrigeration cost increases with refrigeration capacity to the power of 0.6 [3]. The optimum shield thickness,  $t_{so}$ , is then

$$t_{so} = \frac{1}{0.6\mu_s} \text{Log}_e \left[ \frac{0.6\mu_s a_r}{m a_m (r_b + t_s)^{m-1} + 2\pi a_s (r_b + t_s)} \right] \quad (4)$$

Table 1 tabulates  $t_{so}$  for different values of the parameters in eqns. 4. Except for  $\mu_s$ , the dependence of  $t_{so}$  on these parameters is relatively weak. Changing  $m$  from 1 to 2 changes  $t_{so}$  by about 3 to 8%. Doubling the wall radius changes  $t_{so}$  by roughly 2%. The results show a relatively strong dependence on the wall loading. The optimum shield thicknesses are about 67 and 91 cm, respectively, for 70% SS plus 30%  $B_4C$  and 70% Pb plus 30%  $B_4C$ . However, using the Lead- $B_4C$  mixture saves about 18 million dollars compared with the SS- $B_4C$  for a major radius of 13 meters, based on material costs for cases 5 and 7 in Table 1. Furthermore, the optimum shield thickness for Lead- $B_4C$  results in better attenuation than in the SS- $B_4C$  case ( $1.85 \times 10^{-7}$  and  $4.17 \times 10^{-6}$  MeV/MeV).

Table 1 Effect of the Various Parameters on the Values  
of Optimum Shield Thickness

case No.	$r_w$	$r_b$	$\dot{W}_n$ MW/m <sup>2</sup>	m	$a_s^c$ \$/cm <sup>3</sup>	$a_m^d$ \$/cm	$a_r$ \$/cm	$\mu$ cm <sup>-1</sup>	$t_{so}$ cm
1	400	470	0.5	1	0.088 <sup>c</sup>	18.96	3.504(+5)	0.1447 <sup>*</sup>	52.9
2	400	470	1.0	1	0.088	18.96	5.312(+5)	0.1447	57.60
3	400	470	10.0	1	0.088	18.96	2.115(+6)	0.1447	73.19
4	400	470	1.0	2	0.088	0.0339	5.312(+5)	0.1447	57.0
5	400	470	1.0	1	0.0352	18.96	5.312(+5)	0.1447	66.97
6	200	270	1.0	1	0.0352	18.96	3.504(+5)	0.1447	66.65
7	400	470	1.0	1	0.0176	18.96	5.312(+5)	0.1113 <sup>†</sup>	91.06
8	400	470	10.0	1	0.0176	18.96	2.115(+6)	0.1113	111.3

\* corresponds to  $\mu$  for a shield consisting of 70% SS + 30% B<sub>4</sub>C

† corresponds to  $\mu$  for a shield consisting of 70% Pb + 30% B<sub>4</sub>C

c -  $a_s$  of .088 corresponds to 6.4 \$/lb for a density of 6.26 gm/cm<sup>3</sup> (70% SS + 30% B<sub>4</sub>C) and  $a_s$  of .0176 corresponds to 0.92 \$/lb for 70% Pb + 30% B<sub>4</sub>C.

d -  $a_m = \frac{a'_m}{r_{ref}}$  where  $a'_m$  and  $r_{ref}$  were taken as  $70 \times 10^6$  and 5.6 meters [2].

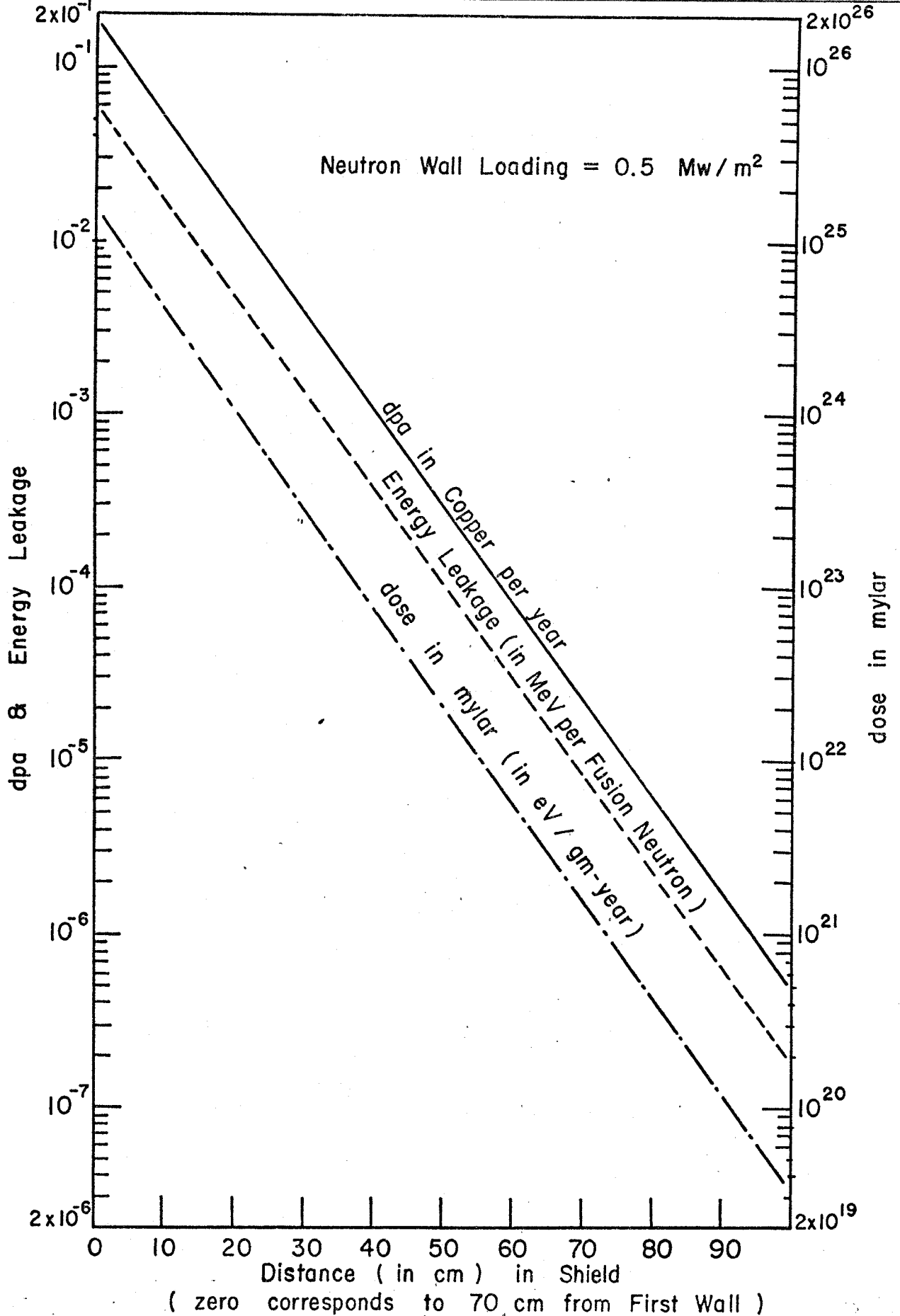


FIG. 1 Comparison of Atomic Displacement in Magnet Stabilizer (Copper) dose in Superinsulation (mylar) & Energy Leakage in a Typical Shield (35%Pb + 35% S.S. + 30% B<sub>4</sub>C)



## References

- [1] M. A. Abdou, "Neutronics and Photonics Design For CTR Blankets and Shields," to be published.
- [2] M. S. Lubell et al, "Economics of Large Superconducting Toroidal Magnets For Fusion Reactors," ORNL-TM-3927 (1972) and I.E.E.E. Conf. Record, I.E.E.E. Cat. No. 72 CHO 682-5 TABSC.
- [3] W. C. Toung and R. W. Boom, "Materials and Cost Analysis of Constant-Tension Magnet Windings For Tokamak Reactors," 4<sup>th</sup> International Magnet Conference, Brookhaven (Sept. 1972)