

*An Approach to Analyzing  
Long Mean-Free-Path Effects on  
First-Wall Ion Threat Spectra*

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HAPL Project Meeting

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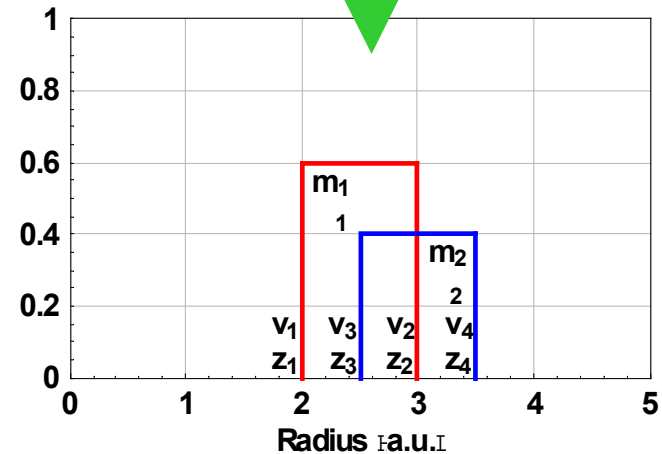
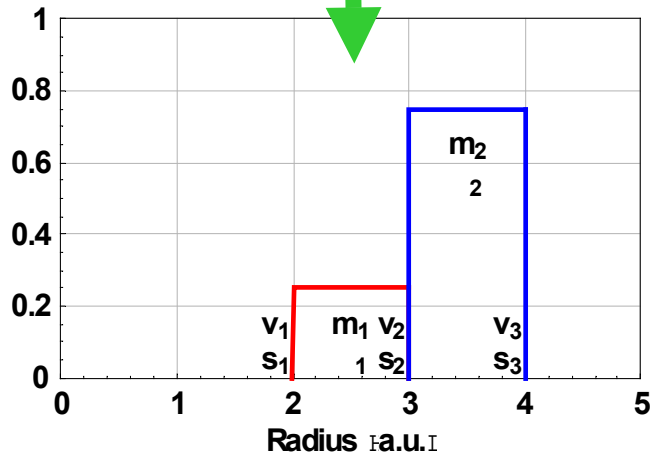
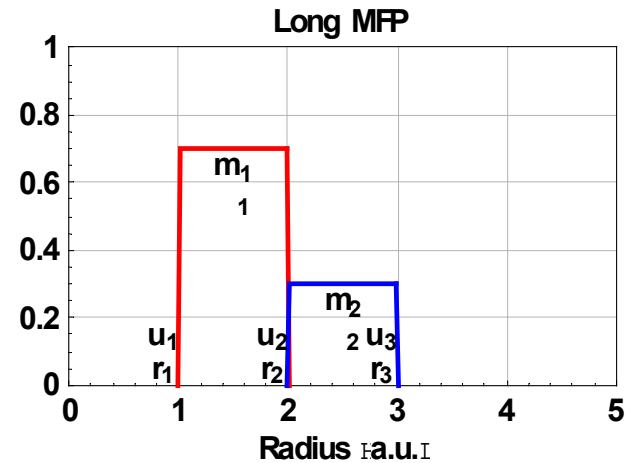
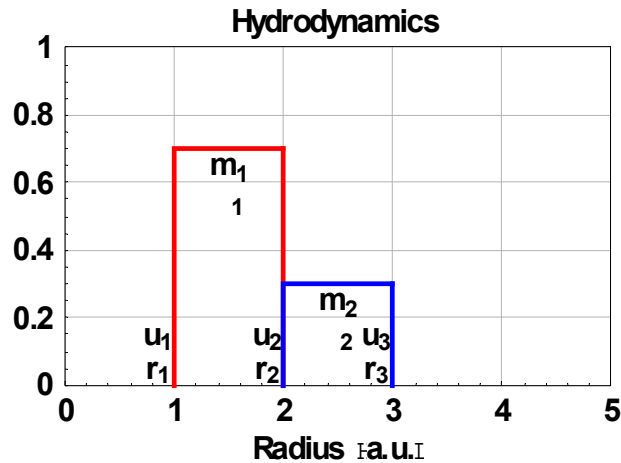
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# Why is Hydrodynamics Not Sufficient for Predicting the Ion Threat Spectra on the First Wall?

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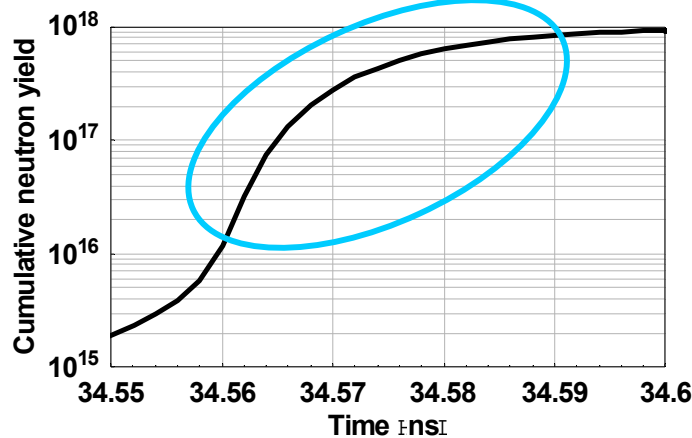
- The hydrodynamic approximation breaks down for particles with mean free paths longer than the scale lengths of interest.
- For HAPL, two classes of ions violate the hydrodynamic assumptions for some fraction of the shot duration:
  - Shock wave passing through background plasma, and
  - Maxwellian ion distribution tails.
- The explosion cannot efficiently accelerate ions with mean free paths longer than the shock thickness or, for some ions, the plasma extent.

# “Perfect” Momentum Transfer Characterizes Hydrodynamics, but Not Long MFP Situations

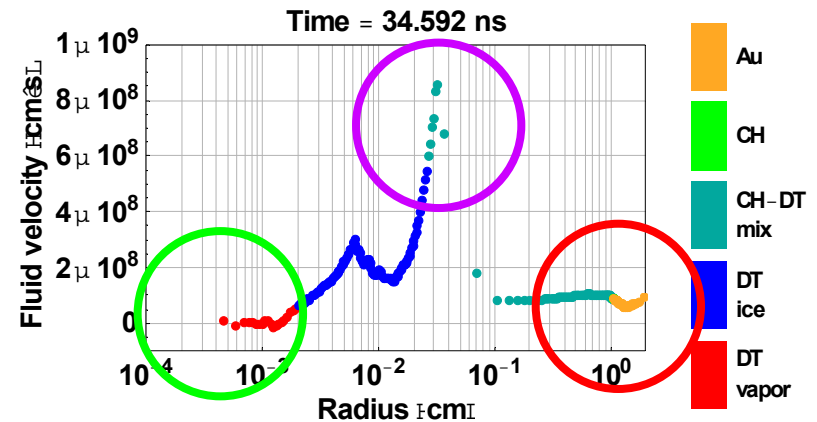
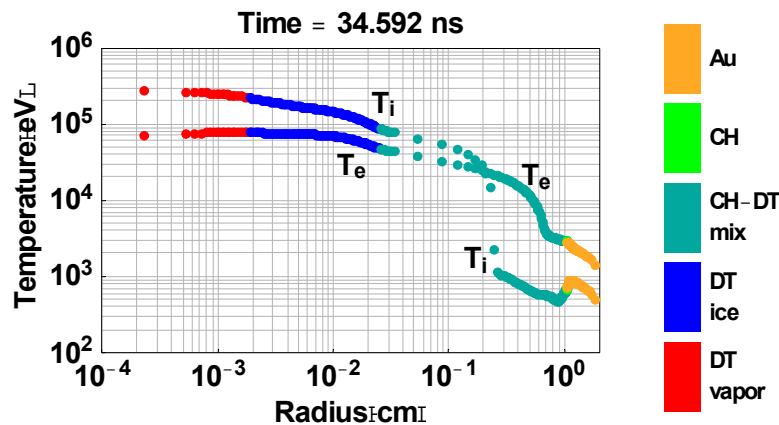
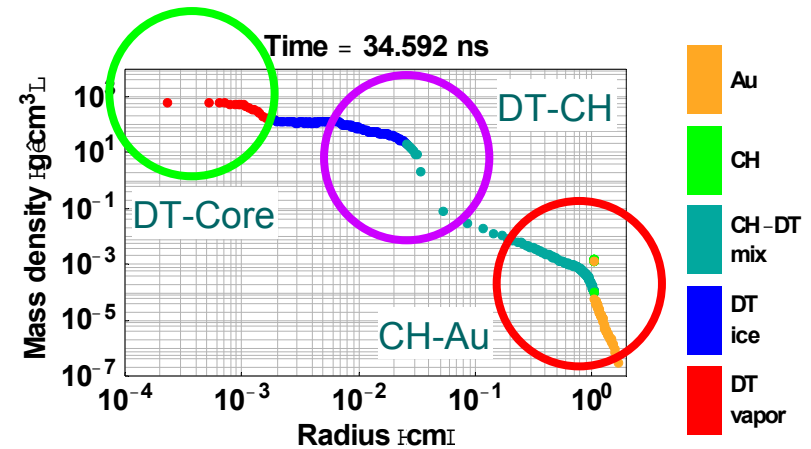


# DT Core, DT-CH Shock, and CH-Au Shock Will Exemplify the Issues

- Neutrons get produced within ~30 ps.



- Each point represents a Lagrangian zone of constant mass.

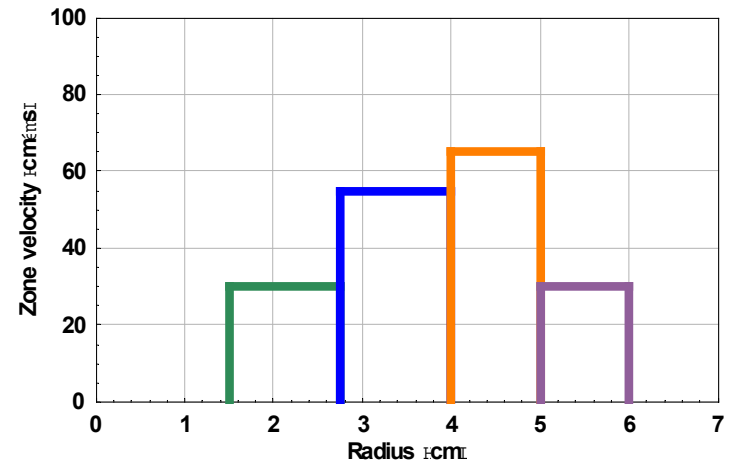
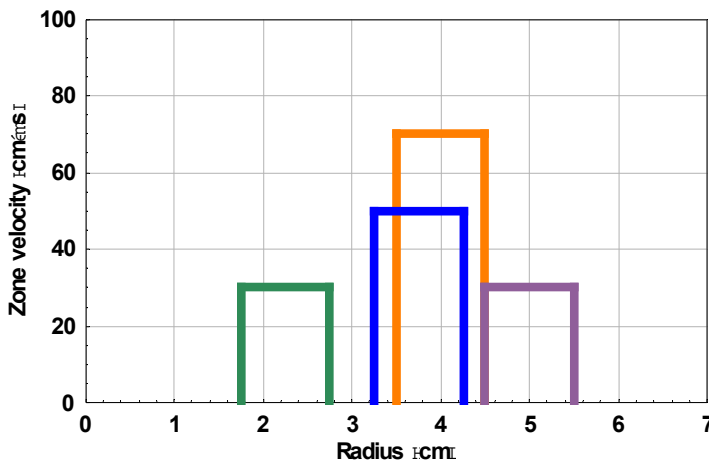
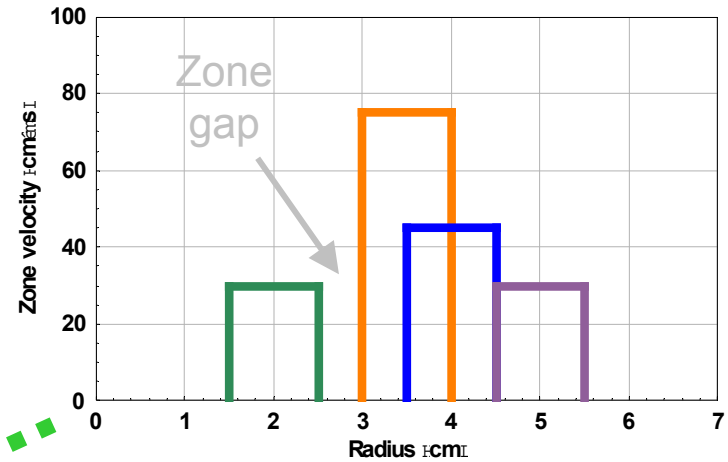
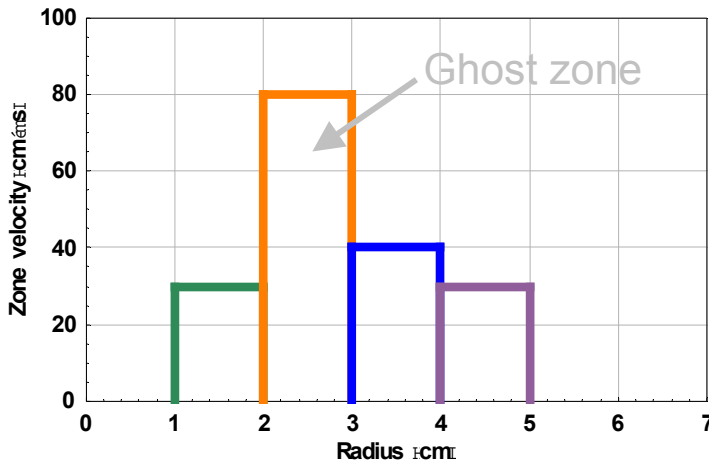


# At 34.592 ns, the DT-CH Shock Thickness and Incoming Ion Mean Free Paths Become Comparable

	DT Core	DT-CH Shock	CH-Au Shock
$r_{\text{shock}}$ (cm)	< 0.001	0.026	1.1
$\Delta r_{\text{shock}}$ (cm)	< 0.001	0.02	0.004
$v_{\text{shock}}$ (cm/s)	$6.6 \times 10^6$	$5.5 \times 10^8$	$8.6 \times 10^7$
$n_i$ (cm <sup>-3</sup> )	$1.5 \times 10^{26}$	$5.1 \times 10^{24}$	$5.0 \times 10^{18}$
$T_i$ (keV)	276	86	2.8
$T_e$ (keV)	72	47	0.69
Ave. charge state	1	DT 1 CH 1	CH 1 Au 36
$\Delta r_{\text{shock}} / \text{mfp}$	> 1000	1.1	0.001

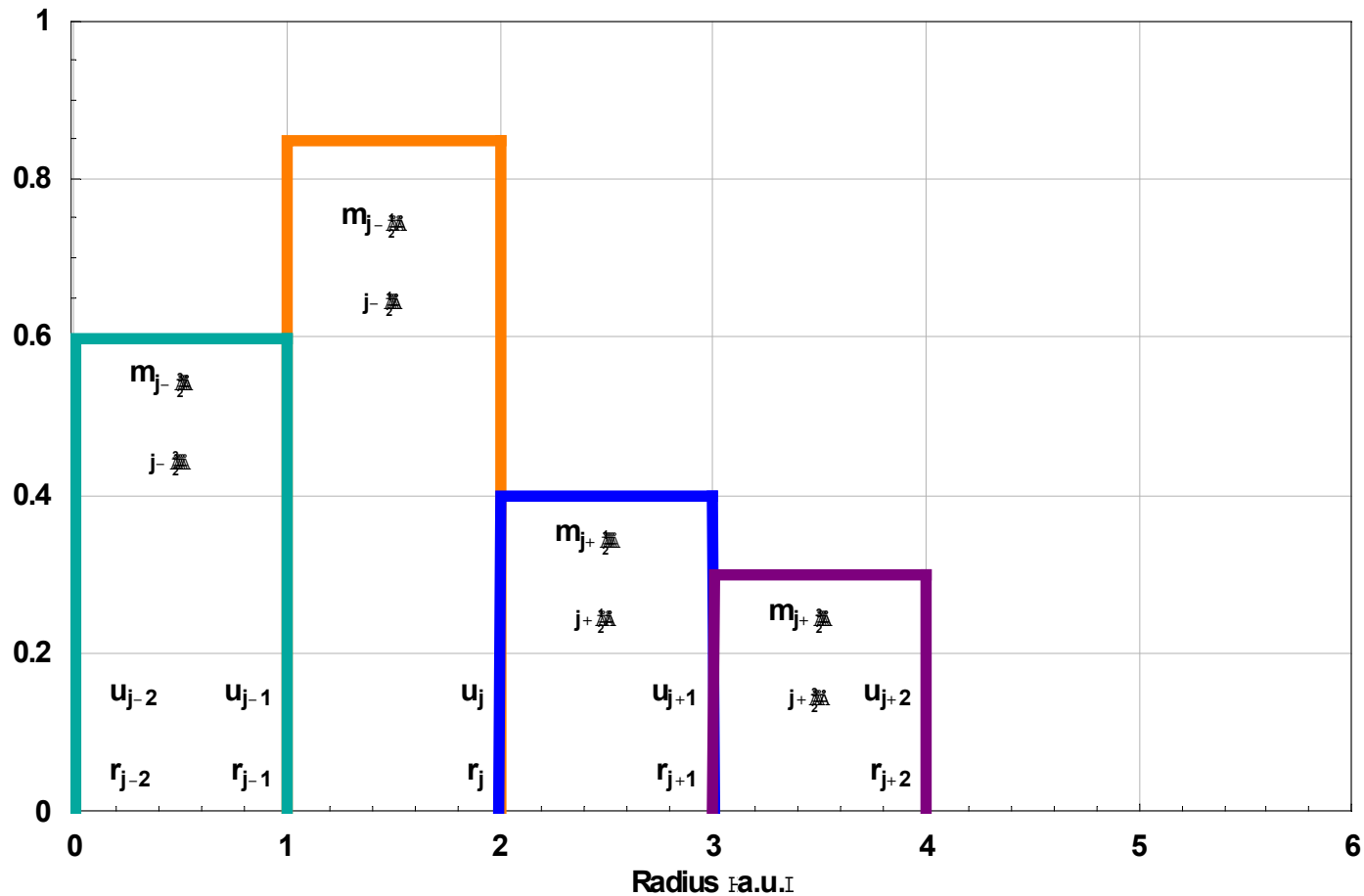
# In the Present Approach, “Ghost” Zones Move through Hydro Zones

- Ghost zones interact with zone boundaries, but only as they pass through them.



# Zone Evolution

- The gold zone is a ghost zone with respect to the blue zone. The green and violet zones always interact in a hydrodynamic manner with all other zones.



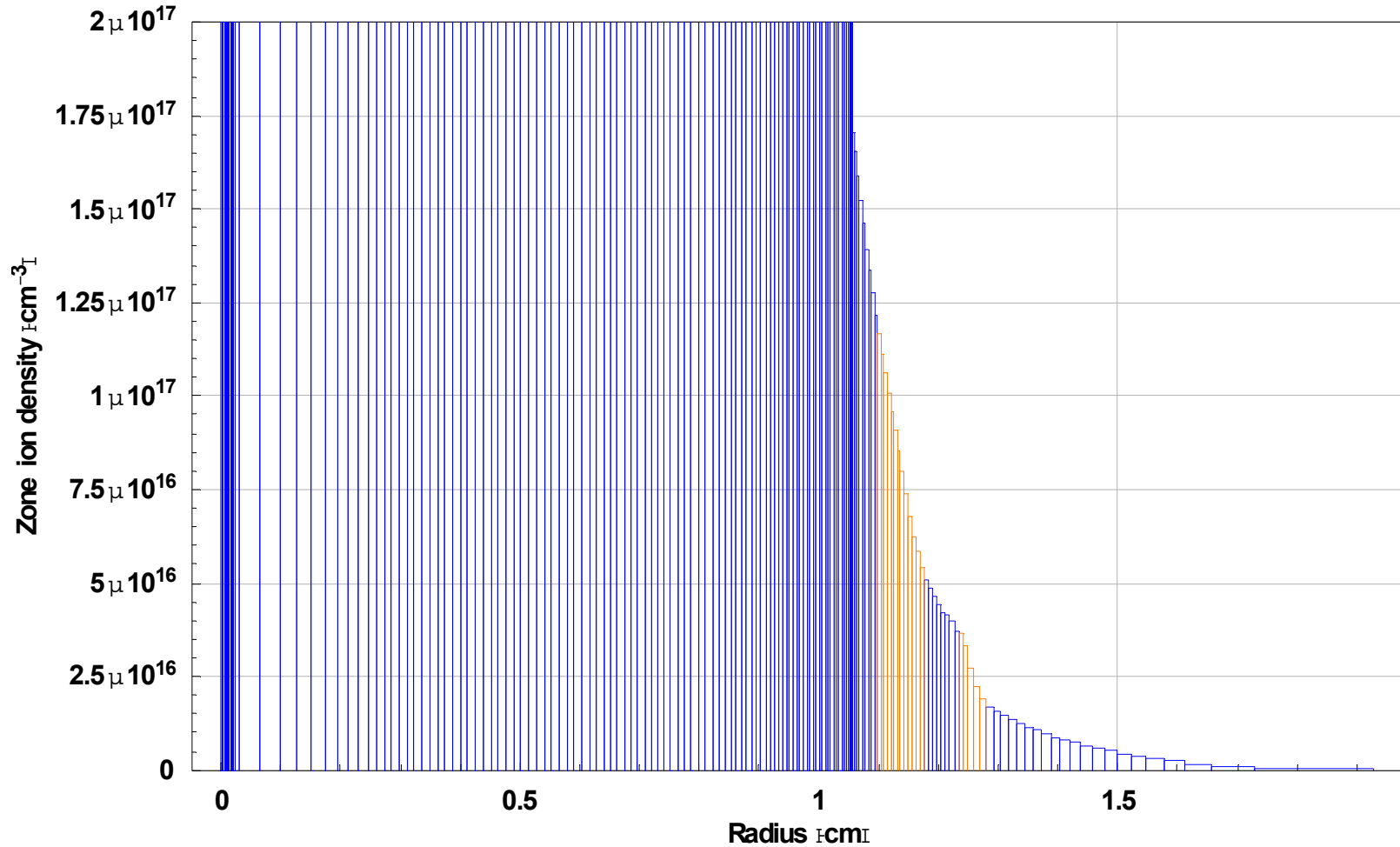
# Computational Approach to Modeling Long Mean-Free Paths

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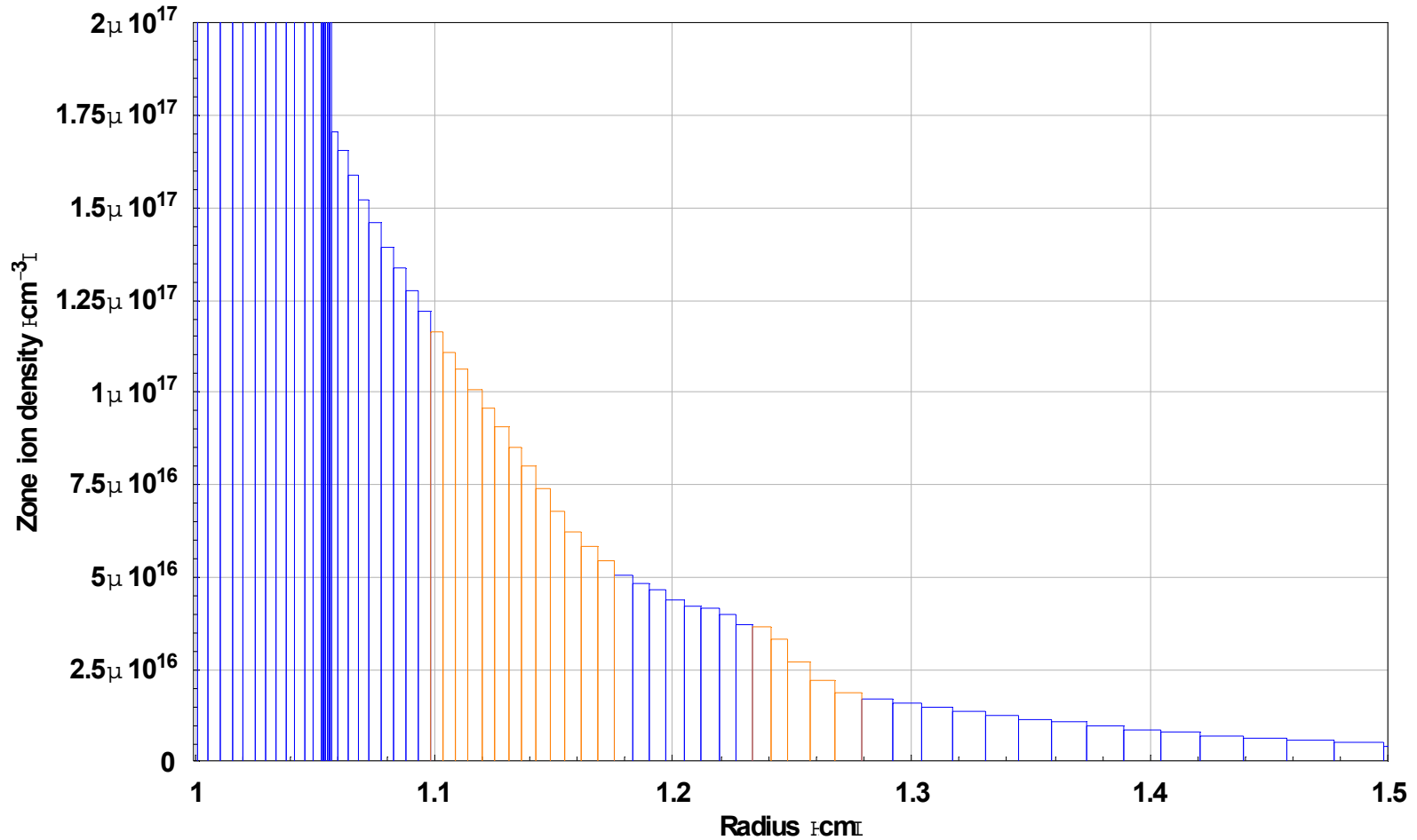
1. Test algorithms in Mathematica<sup>®</sup> using a simplified Lagrangian code  $[\partial u / \partial t + \partial p / \partial m = 0; \partial e / \partial t + p(\partial V / \partial t) = 0]$ :
  - a. Perform zone-by-zone check for long mean-free path zones (*ghosts*) relative to adjacent zones.
  - b. Move ghost zones a hydro time step  $dt$  through a series of partial time steps,  $\delta t$ , set by intersecting zone boundaries.
    - Check ghost/hydro status at each  $\delta t$ .
  - c. Move hydro zones for time step  $dt$ .
  - d. Update plasma, control, and time parameters.
  - e. Reattach ghost zones that return to hydro status & renumber.
2. Implement modified algorithms in BUCKY.



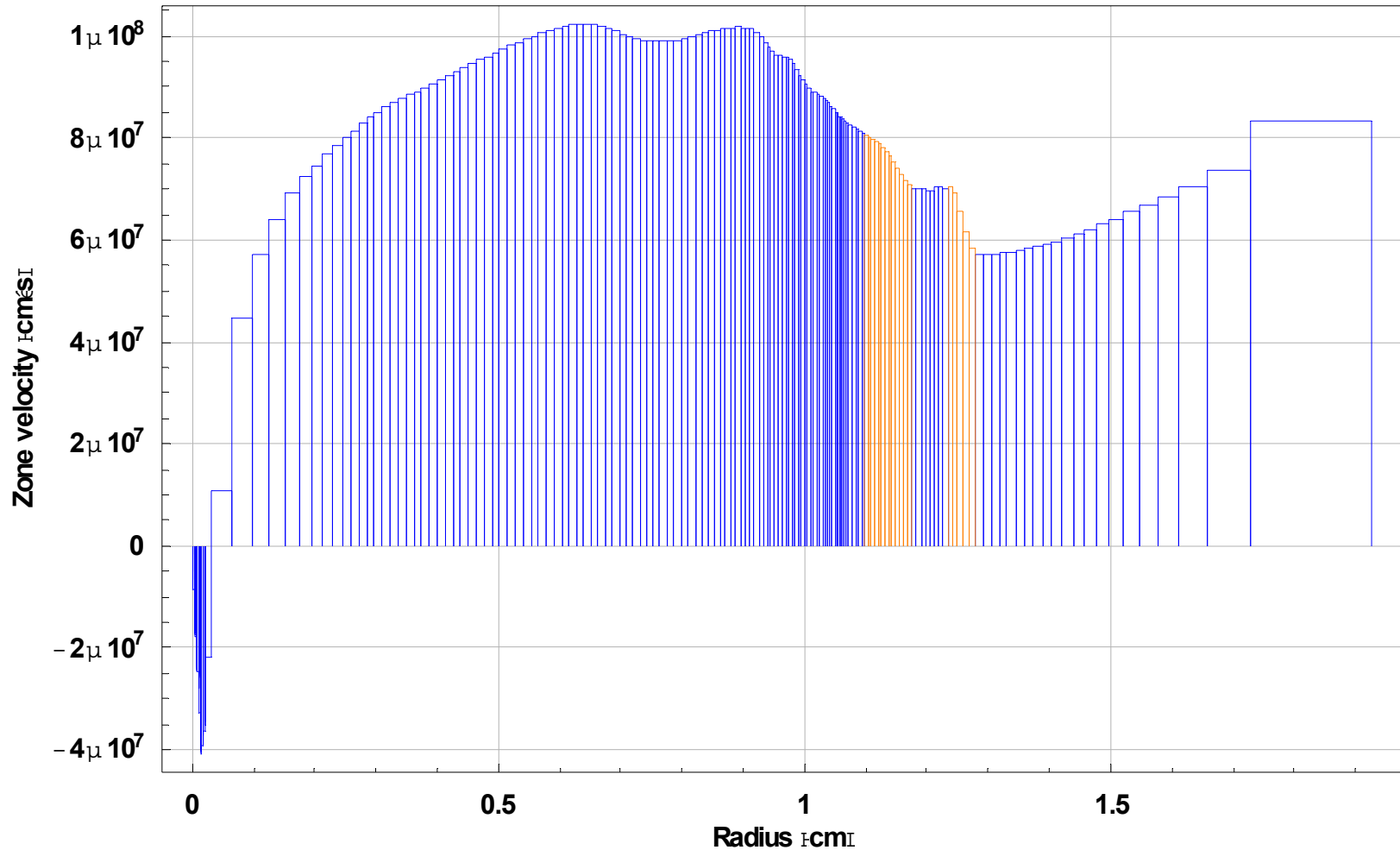
# Lagrangian Zone Ion Density Falls Steeply in the



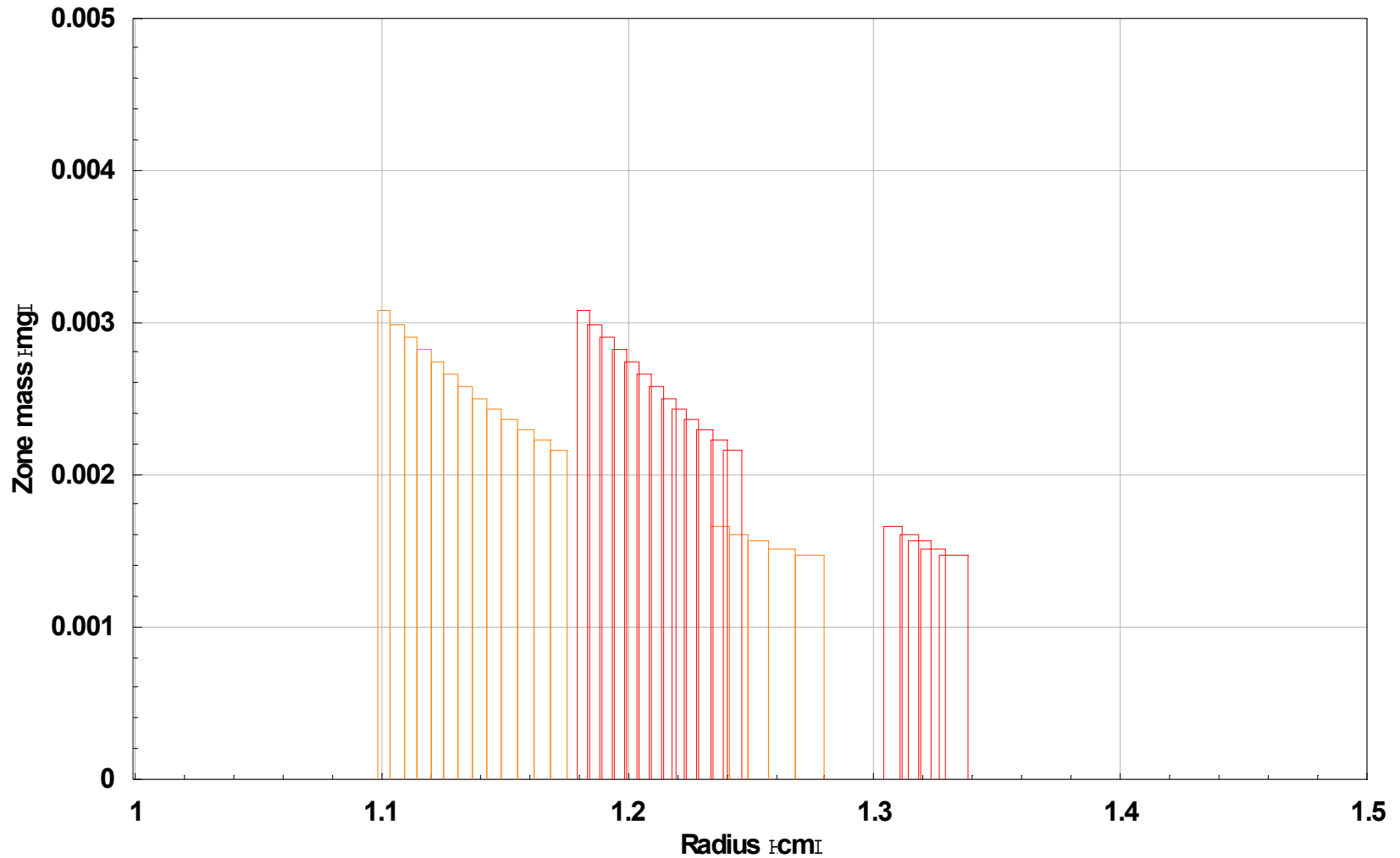
# Lagrangian Zone Evolution for Mean Free Paths $\gtrsim$ Shock Thickness



# Lagrangian Zone Evolution for Mean Free Paths $\gtrsim$ Shock Thickness



# Lagrangian Zone Evolution for Mean Free Paths $\gtrsim$ Shock Thickness



# Status and Summary

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- Developed an algorithm for velocity transfer between zones of long relative mean-free paths.
- In final stages of debugging this method in a Mathematica<sup>®</sup> code, originally written for simplified hydrodynamics:
  - Zel'dovich and Raizer problem of supernova shock wave into an exponentially decreasing stellar atmosphere.
  - HAPL problem, starting  $\sim 30$  ps after start of burn.
- Work remains to implement the long mfp algorithms in BUCKY, in order to include radiation transfer, equations of state, and other effects.