

# Portfolios & Systematic Risk

## Expected Return and Variance of a Portfolio

$$E(R) = w_i E(r_i)$$

$$V(R) = w_i w_j \text{Cov}(r_i, r_j)$$

## The Variance Contributed by Stock $i$

$$\begin{aligned} w_j \text{Cov}(r_i, r_j) &= \text{Cov}(r_i, w_j r) \\ &= \text{Cov}(r_i, r_m) \end{aligned}$$

# Portfolios & Systematic Risk

**Stocks with *small* or *negative* covariances with the market:**

- 1. will reduce portfolio risk**
- 2. will be demanded by investors.**

**Systematic risk determines value**

# Residual Risk: Why it Does Not Affect Value

## Return Model for Securities

Return on security  $i$ :  $r_i = \alpha_i + \beta_i r_m + \epsilon_i$

Return on security  $j$ :  $r_j = \alpha_j + \beta_j r_m + \epsilon_j$

$$E(\epsilon_i) = E(\epsilon_j) = 0, \text{Cov}(\epsilon_i, \epsilon_j) = 0$$

## Expected Returns, Variances & Covariances

$$E(r_i) = \alpha_i + \beta_i E(r_m)$$

$$\text{Var}(r_i) = \beta_i^2 \text{Var}(r_m) + \text{Var}(\epsilon_i)$$

$$\text{Cov}(r_i, r_j) = \beta_i \beta_j \text{Var}(r_m)$$

# Mean & Variance of Portfolio Returns

**Form an Equally Weighted Portfolio of  $n$  Stocks**

$$R = (1/n) \sum_{i=1}^n r_i = (1/n) \sum_{i=1}^n (r_i + r_m) + (1/n) \sum_{i=1}^n r_m$$
$$\text{Var}(R) = (1/n)^2 \sum_{i=1}^n \text{Var}(r_i) + (1/n)^2 \sum_{i=1}^n \text{Var}(r_m)$$

**Residual risk is “diversified away” in a portfolio.  
Therefore it has no effect on the cost of capital.**

# Calculating the Cost of Equity

**Cost of equity=risk free rate+Risk premium**

$$r_e = r_f + (E(r_m) - r_f)$$

where  $r_f$  is the risk free rate, and  $E(r_m)$  is the return on the market portfolio.

is the measure of systematic risk

$$=Cov(r_e, r_m)/Var(r_m)$$

# *Value of a Stock*

**large covariance with the market**

*implies*

**large Beta**

*implies*

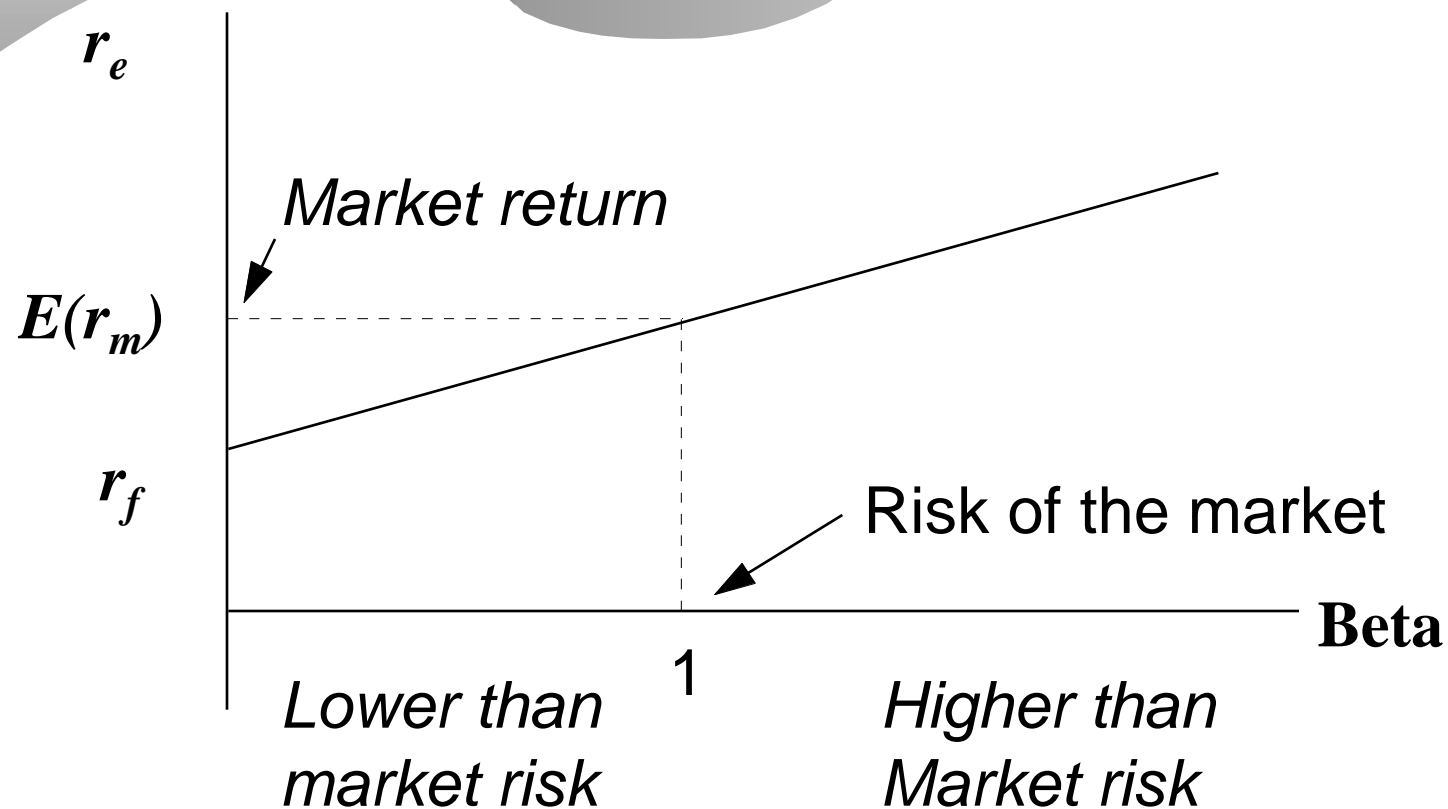
**high cost of capital**

*implies*

**low stock price**

**Stock price=  $E(\text{Cash Flow})/(1+r_i)^t$**

# Calculating the Cost of Equity



# Some Betas

<u>Company</u>	<u>Beta</u>	<u>COC</u>
Grumman	0.617	<Market
Honeywell	1.045	=Market
Scientific-Atlanta	1.541	>Market
Cyprus Minerals	1.200	>Market
Ashland Coal	0.650	<Market
Intel Corp	1.435	>Market
Wisc Energy	0.565	<Market

Source *Value Line, QuoteCom*





## **Application to lunar mining of Helium-3**

*How would a market for  $^3\text{He}$  be organized?*

*What would be the cost of capital to a lunar mining company?*

*How much financing would be required?*

*Could the capital be raised?*

*Can  $\text{D}^3\text{He}$  fusion generated power compete?*

# *Cost of Capital for a Lunar Mining Company*

## **Residual Risk**

Related to lunar mining operations

May be substantial

Can be diversified away in investor portfolios

## **Systematic Risk**

Related to the sales of electricity

Should be comparable to fuel suppliers to electric utilities and aerospace companies

Cannot be diversified away in investor portfolios

## **Cost of Capital**

Should be comparable to fuel suppliers and aerospace companies

# *D<sup>3</sup>He Penetration in US Electricity Market*

<b>Year</b>	<b><i>Predicted % of US Energy Generated by DHe3 Fusion</i></b>
<b>2015</b>	<b>0.03%</b>
<b>2020</b>	<b>0.41%</b>
<b>2025</b>	<b>1.80%</b>
<b>2030</b>	<b>7.19%</b>
<b>2050</b>	<b>60.27%</b>

From Thompson, Ott, Kulcinski “*Economic Analysis of the Use of Lunar Helium-3 as a Fuel in U.S. Energy Policy,*” Wisconsin Working Paper 3-90-5, 1990

# *Financing the Lunar Mining Company: Production of $^3\text{He}$*

## Projected Investment in Mining Machines

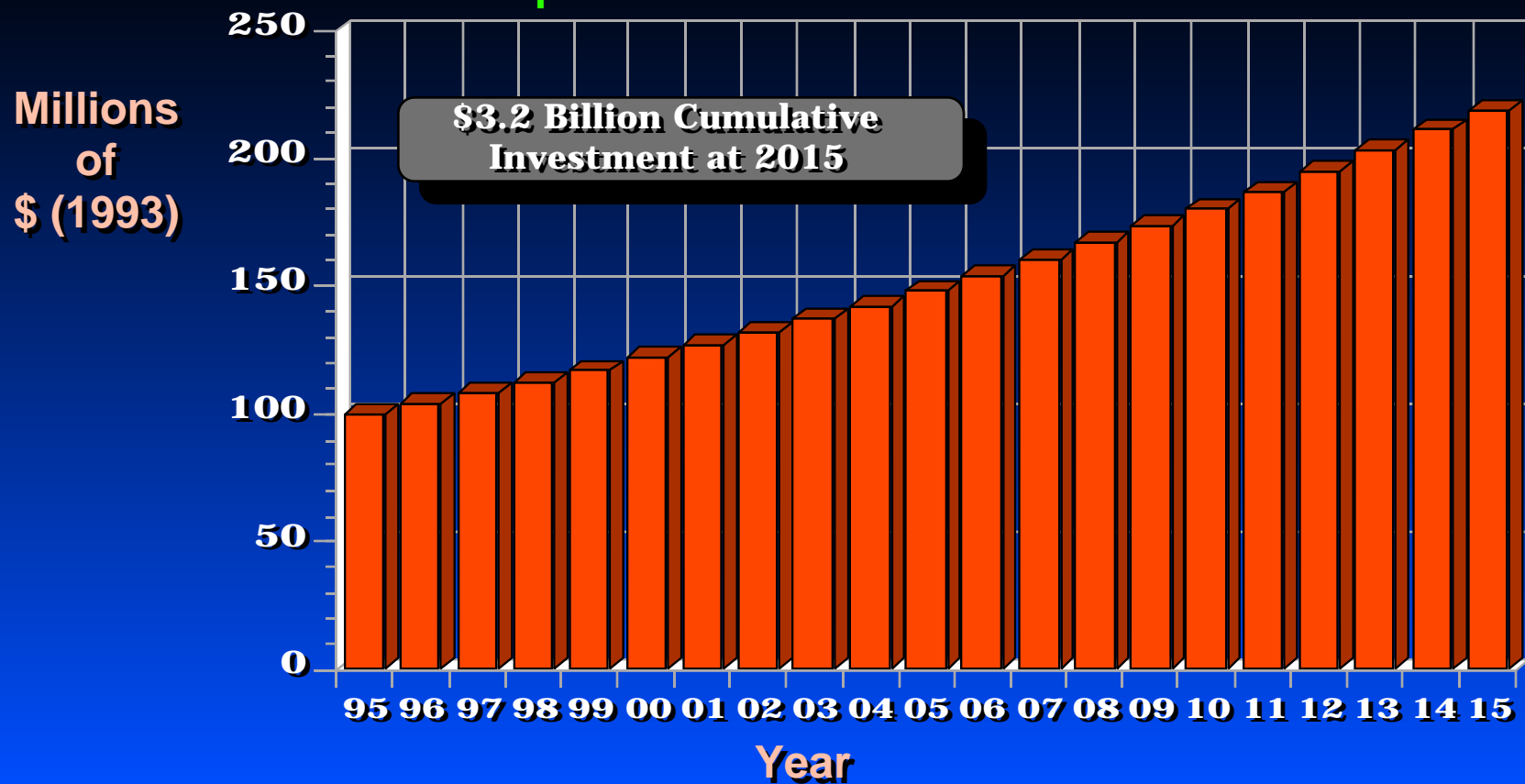
<i>Year</i>	<i>Mach.</i>	<i>Mach Invest</i>	<i>Launch Invest</i>	<i>Total Invest</i>
2015	1	\$ 10M	\$ 50M	\$ 60M
2020	10	\$ 100M	\$ 500M	\$ 600M
2025	57	\$ 570M	\$ 2,850M	\$ 3,420M
2030	230	\$ 2,300M	\$11,500M	\$13,800M
2050	2050	\$20,500M	\$102,500M	\$123,000M

Investment per miner-\$10,000,000

Launch cost per miner \$50,000,000

# Financing the Lunar Mining Company: R&D

Lunar Mining R&D for  $^3\text{He}$  Procurement Over and Above R&D Required for a Lunar Scientific Base



# *Private Financing of Large Projects Is Possible...*

## Some Large Projects

<u>Investor (Year, Project)</u>	<u>Size</u>
<b>Globalstar (1996)</b> <b>(Satellite Communications)</b>	<b>\$ 2.00B</b>
<b>General Electric (1986)</b> <b>(Acquisition of RCA)</b>	<b>\$ 6.14B</b>
<b>KKR (1989)</b> <b>(Takeover of RJR Nabisco)</b>	<b>\$26.4B</b>

# *...But Large Losses Can be Devastating*

## Orange County, CA (1994)

- ~\$1.7B loss on municipal investment pool
- ~Filed for reorganization under Chapter 9,  
Federal Bankruptcy Reform Act of 1978

## Barings Bank (1995)

- ~Nicholas Leeson lost \$1.3B on a derivative  
gamble
- ~Barings bank ceased to exist as an  
independent unit

# *Two Financing Plans*

① *Government finances R&D; private enterprise finances production*

② *Private enterprise finances R&D and production*

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***Are they feasible?***



## ① *Government-Private*

- ✓ **Government** pays *R&D 1996-2015* in return for the *by-products of lunar mining after 2015*.
- ✓ **Lunar mining Company** finances *miner purchases, launches, and mining operations starting in 2015 and recovers  $^3\text{He}$ . Supplies by-products to the government after 2015*.

# ① Government-Private

## ◆ **Government**

- *\$3.2B spent between 1996 and 2015*
- *Return on investment delayed until after 2015*
- *Taxing power used to raise funds*
- ***Maximum losses to taxpayers are small***

## ◆ **Lunar Mining Co**

- *No investment required until 2015*
- *Return on investment begins in 2015 when  $^3\text{He}$  is recovered and sold to electric utilities*
- ***Minimum risks to investors***

## ② *Private Only*

### ✓ **Lunar Mining Company**

- *finances R&D 1996-2015*
- *finances miners, launches, and production after 2015*
- *recovers and sells both  $^3\text{He}$  and by-products*

### ✓ **Government**

- *buys by-products from Lunar Mining Company after 2015*

## ② *Private Only*

### ◆ **Lunar Mining Co**

- *\$3.2B investment*  
*1996-2015 produces*  
*no return until 2015*
- *<sup>3</sup>He sales price must*  
*include R&D costs*
- *Risks relating to by-*  
*product sales*
- ***High risk venture***  
***with questionable***  
***profitability***

### ◆ **Government**

- *Smaller tax revenues*  
*needed 1996-2015*
- *Moon bases must be*  
*supplied from earth*  
*with high cost*  
*launches*
- ***Increased cost of***  
***space programs***

# Government-Private

## General Assumptions

- **Scientific Base on the Moon Established by Government**
- **An Investor Owned Lunar Mining Company Exists**
  - **Holds a U.S. Franchise for Mining  $^3\text{He}$  on the Moon**
  - **Responsible for Transport of Equipment to and  $^3\text{He}$  from the Moon**
  - **Markets  $^3\text{He}$  Fuel to Utilities**
  - **Is Financed Entirely with Equity Capital**
  - **Seeks to Earn a Return Commensurate with Risks**
- **Government Agencies Fund Lunar Mining R&D in Return for Free Volatile By-Products**
- **First  $^3\text{He}$  Mining in 2015**

# Government-Private

## Expenditure Categories Used to Analyze the Cost of $^3\text{He}$

### *Operating Cost Categories*

- Mining Equipment, Labor, and Habitat Costs
- Launch Costs
- Required Profits
- Income Taxes

### *Development Cost and Cost Offset Categories*

- Research and Development Costs
- Cost Offsets from Volatiles

# Government-Private

## Assumptions Regarding Mining Operating Starting in 2015 (cost in 1993\$)

<b>Launch Costs</b>	<b>\$1000/kg</b>
<b>Miner Mass</b>	<b>50 tonnes</b>
<b>Miner Economic Life</b>	<b>20 years</b>
<b>Miner Capacity</b>	<b>33 kg of <sup>3</sup>He/year/miner</b>
<b>Miner Purchase Price</b>	<b>\$10,000,000</b>
<b>Labor Force on the Moon</b>	<b>3 persons/miner</b>
<b>Salary and Fringe Benefits</b>	<b>\$500,000/person/year</b>
<b>Habitat and Consumables</b>	<b>820 kg/person/year</b>
<b>Miner Depreciation</b>	<b>Straight Line, 20 years</b>
<b>Miner Launch Cost Amortization</b>	<b>Straight Line, 20 years</b>
<b>Income Tax Rate</b>	<b>36%</b>

## ① Government-Private

### Yearly Required Revenue Per Miner (Habitat+Labor+Profit+Taxes+Depreciation)

$$R = aH + aL + \left[ \frac{L_m + M}{pvf} - D \right] + \frac{1}{1 - \text{income tax rate}} \left[ \frac{L_m + M}{pvf} - D \right] + D$$

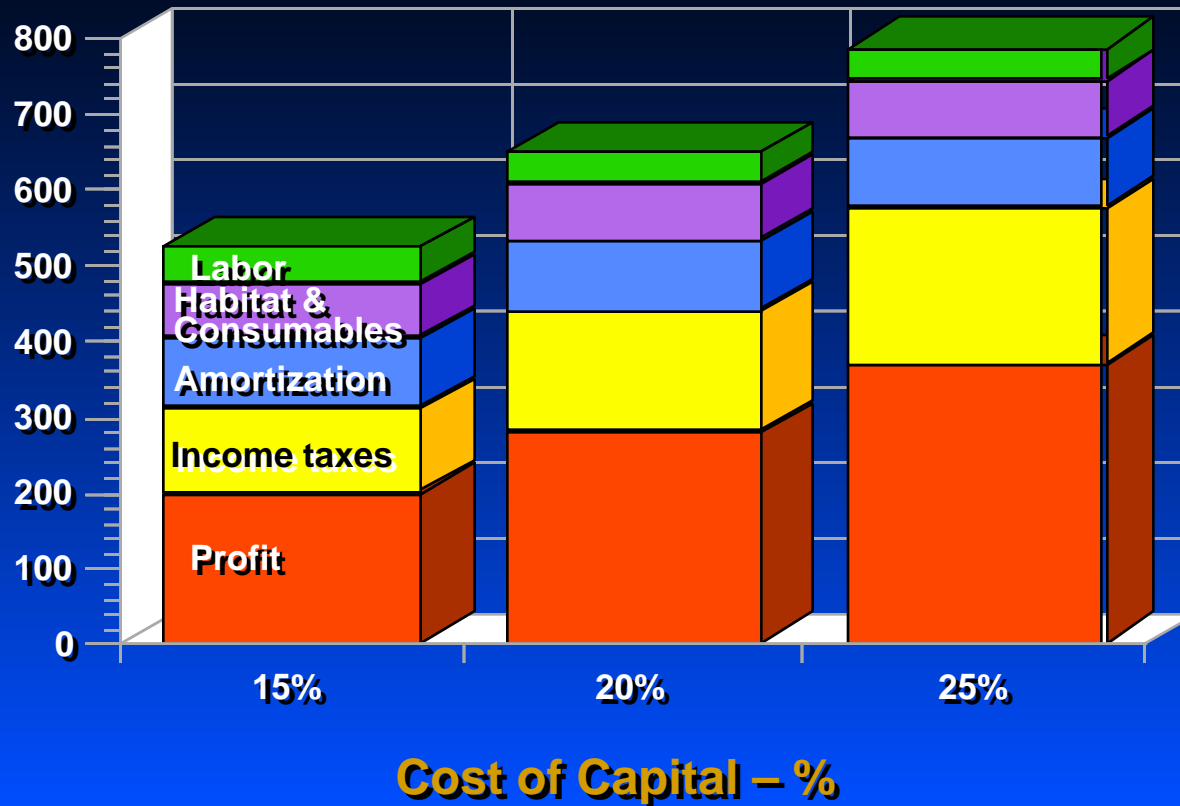
*H=habitat cost/person /yr, L=salary+fringe/person/yr, L<sub>m</sub>=miner launch cost, M= miner initial cost, D= Yearly depreciation=(L<sub>m</sub>+M)/n , n=miner life, = income tax rate, pvf=present value factor, a=Number of astronauts*



# ① Government-Private

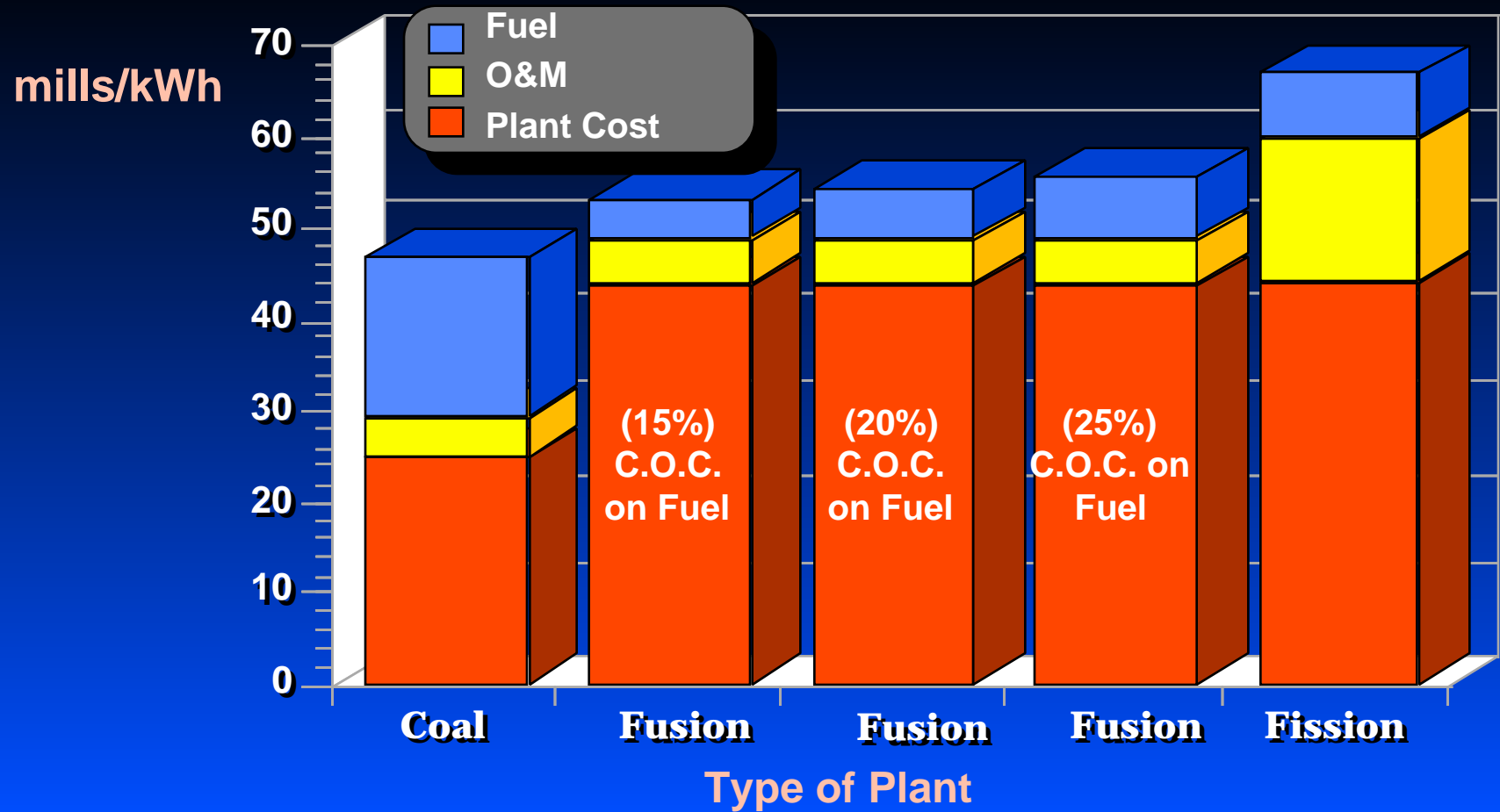
## Cost of Helium-3 (Including the Cost of Capital)

Cost of Helium-3 per Gram (\$1993)



## ① Government-Private

### Cost of Electricity Produced by Coal, D<sup>3</sup>He Fusion and Fission



## ① Government-Private

# Sensitivity of Price of $^3\text{He/g}$ to Cost Elements

(15% Cost of Capital)

<i>Launch Cost/kg</i>	<i>Price of <math>^3\text{He/g}</math></i>
<i>\$1000</i>	<i>\$523</i>
<i>\$1500</i>	<i>\$728</i>
<i>\$2000</i>	<i>\$933</i>

<i>Number of Astronauts</i>	<i>Price of <math>^3\text{He/g}</math></i>
<i>3</i>	<i>\$523</i>
<i>6</i>	<i>\$568</i>
<i>9</i>	<i>\$613</i>

## ① Government-Private

# The Role of By-Products from $^3\text{He}$ Mining

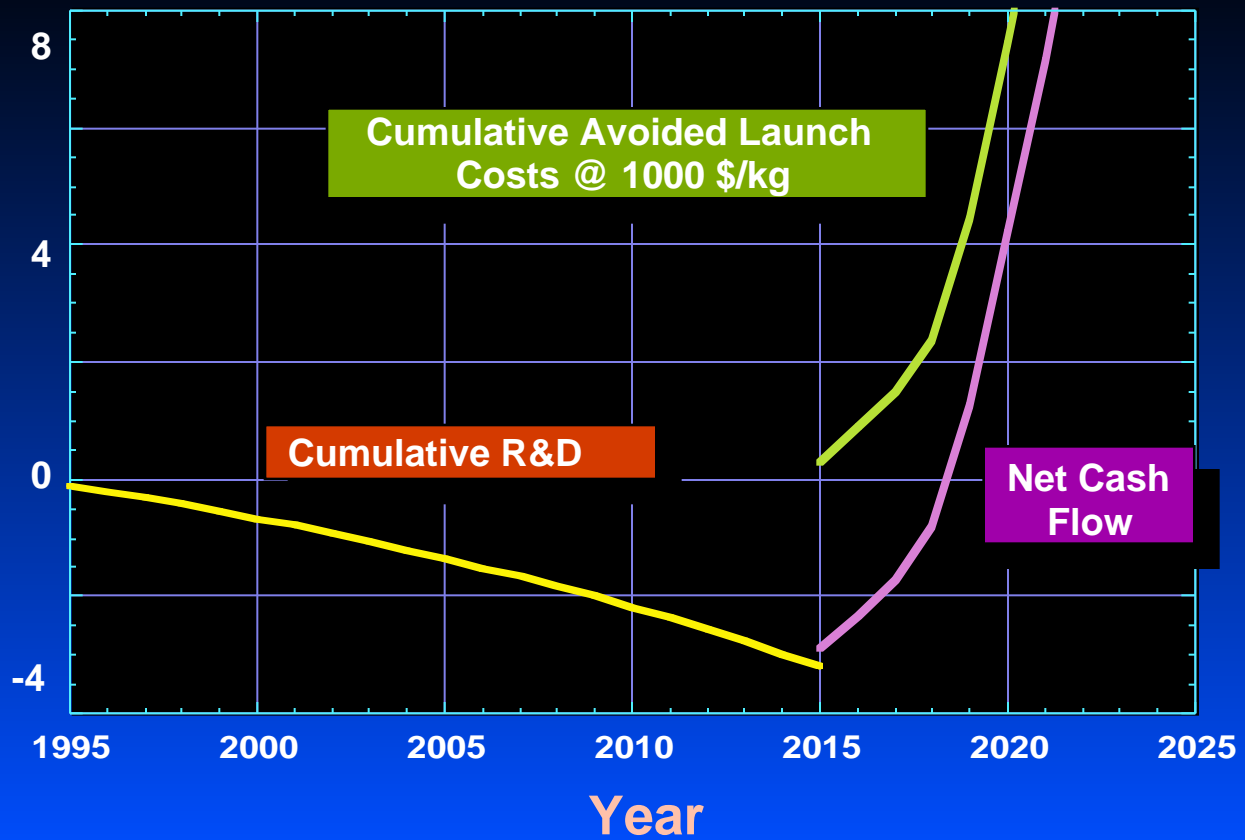
- ✓ 18,200kg Volatile By-Products/kg  $^3\text{He}$
- ✓ 600,600kg of By-Products per miner per year
- ✓ Assume Government Uses 30% of the By-Products
- ✓ **Launch Costs Saved per miner per year =**  
**\$180,180,000**

<b>Year</b>	<b>Miners</b>	<b>Yearly Savings</b>
2015	1	\$ 180,000,000
2020	10	\$ 1,180,000,000
2025	57	\$10,270,260,000

# ① Government-Private

## Net Cash Flow to Government

Billions of  
\$ (1993)



## ① *Government-Private*

### **Conclusions**

- **If the Government Funds all *Additional Lunar Mining R&D***

- **An adequate profit incentive for a Lunar Mining Company exists**

- **The selling price to utilities will be between \$500/gram and \$800/gram**

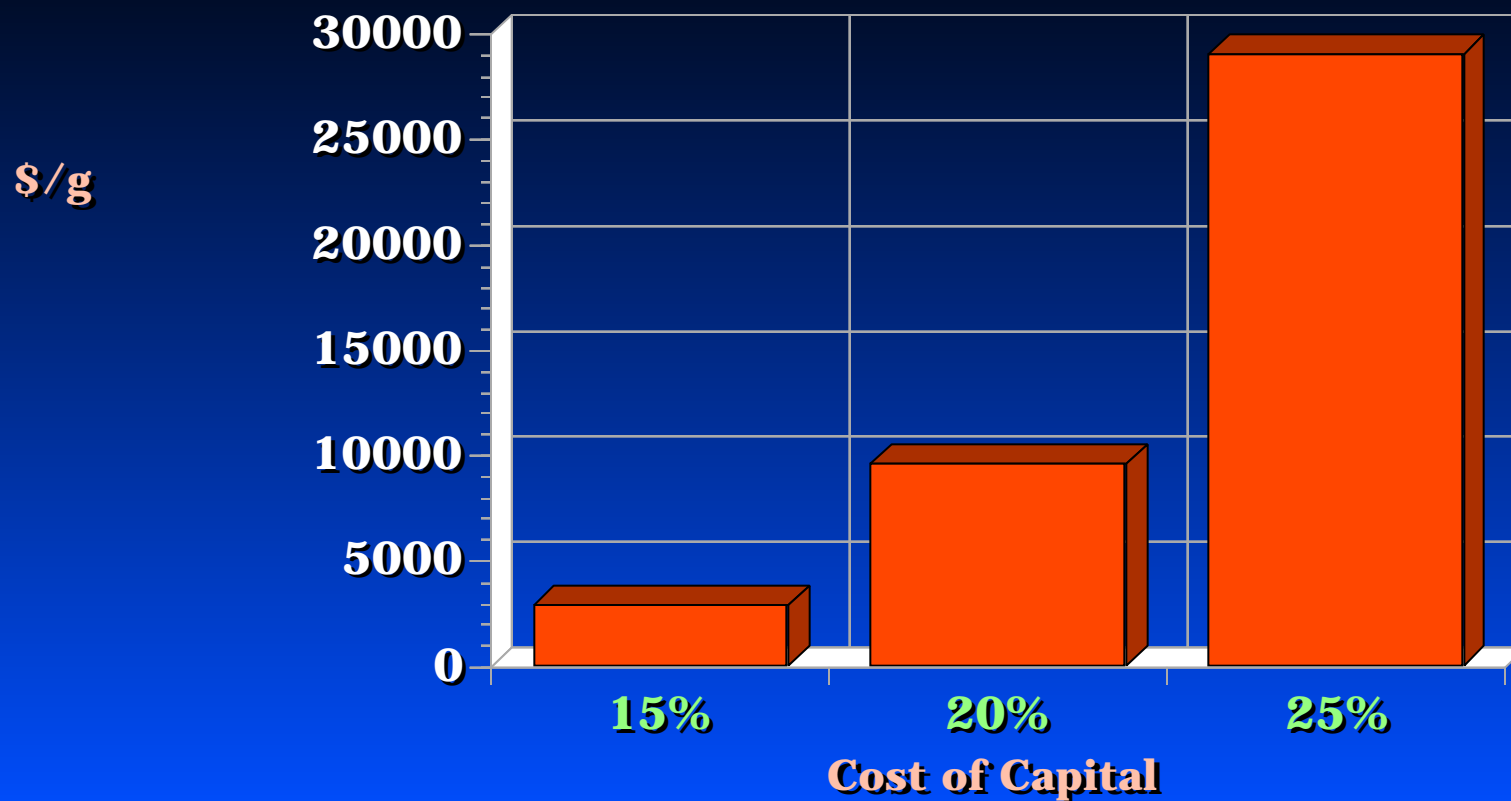
- **Electricity cost from  $^3\text{He}$  fusion power plants will be competitive with coal and fission**

- **The government will recover its R&D expenditures by 2020**

- **The government will earn a substantial return ( 20%) on its investment**

## ② *Private Only*

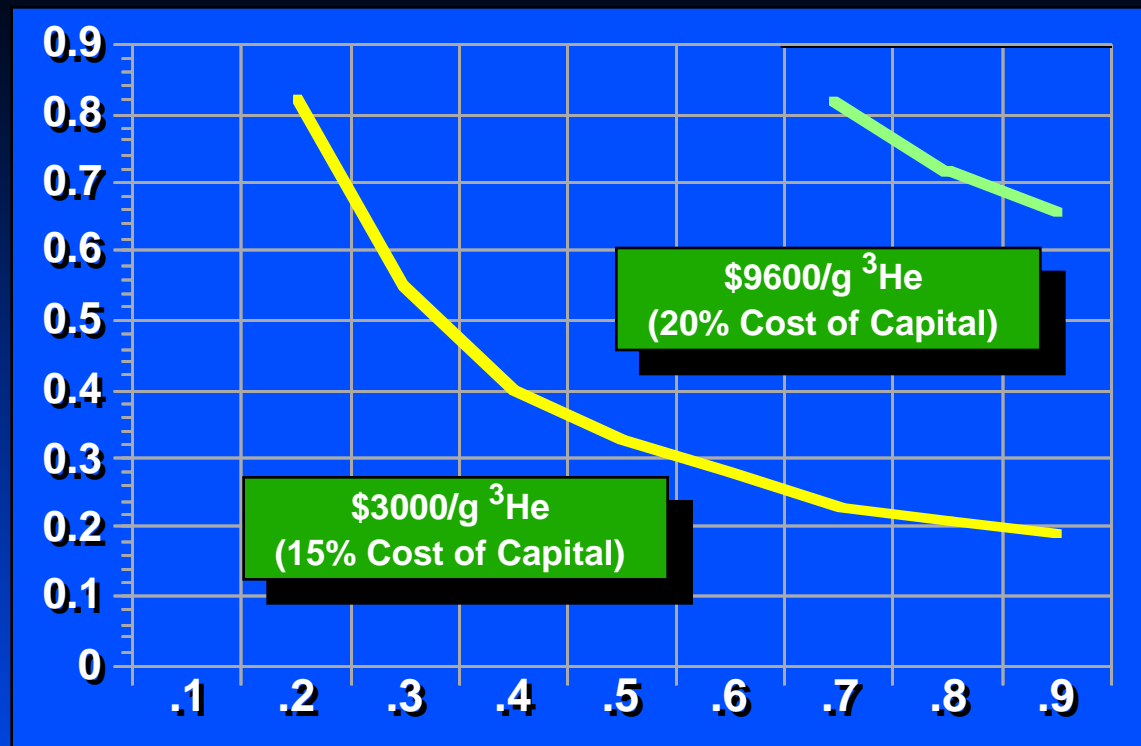
**R&D Component of Cost of  $^3\text{He}$  (\$/g) If Lunar Mining Company Bears All R&D Funding**



## ② Private Only

### Volatiles Sales Needed to Offset Additional Space R&D

Price as a  
Fraction of  
Launch  
Costs



Fraction of Volatiles Sold to Bases



## *Can the funds be raised for financing of the Lunar Mining Co., Inc.?*

- ◆ *The key element is financing R&D*
  - *Funding amounts are large but manageable*
  - *Substantial risk for private investors*
    - ◆ *20 years of cash outlays before a cash inflow*
    - ◆ *By-product sales needed to make  $^3\text{He}$  competitive*
    - ◆ *Uncertainty of market for the by-products*
- ◆ *Government risks are minor in **government-private** undertaking*

## References

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Keown, Scott, Martin, Petty, *Basic Financial Management, 7th ed.* Prentice-Hall 1996

Bodie, Kane, Marcus, *Investments*, 3rd ed. Irwin, 1996

Greenberg, Hertzfeld, *Space Economics*, Vol 144, Progress in Astronautics and Aeronautics, American Institute of Aeronautics and Astronautics, 1992

Thompson, "Cost of  $^3\text{He}$  from the Moon," *Second Wisconsin Symposium on Helium-3 and Fusion Power*, Wisconsin Center for Space Automation and Robotics, July 1993, p.159-172

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