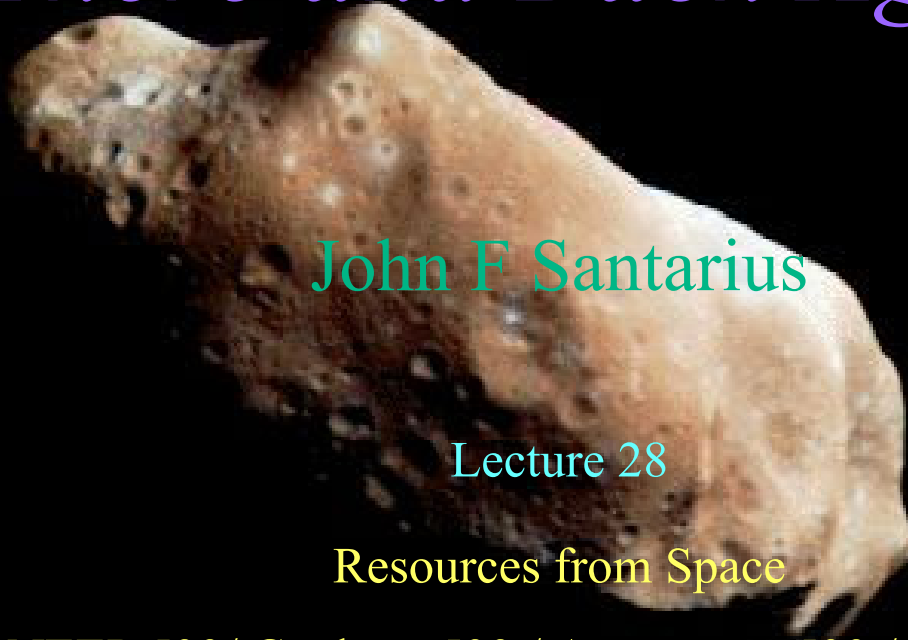


# *Travel to Asteroids and Moons*

## *There and Back Again!*



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Resources from Space

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# Launching from Moons Is Relatively Easy, but Planetary Gravitational Fields Can Be Large

<i><b>Moon</b></i>	<i><b>Surface escape <math>\Delta v</math> (km/s)</b></i>	<i><b>Planet escape <math>\Delta v</math> (km/s)</b></i>
Moon (Earth)	2.37	1.44
Io (Jupiter)	2.56	24.5
Europa (Jupiter)	2.02	19.4
Ganymede (Jupiter)	2.74	15.4
Callisto (Jupiter)	2.44	11.6
Titan (Saturn)	2.54	7.88

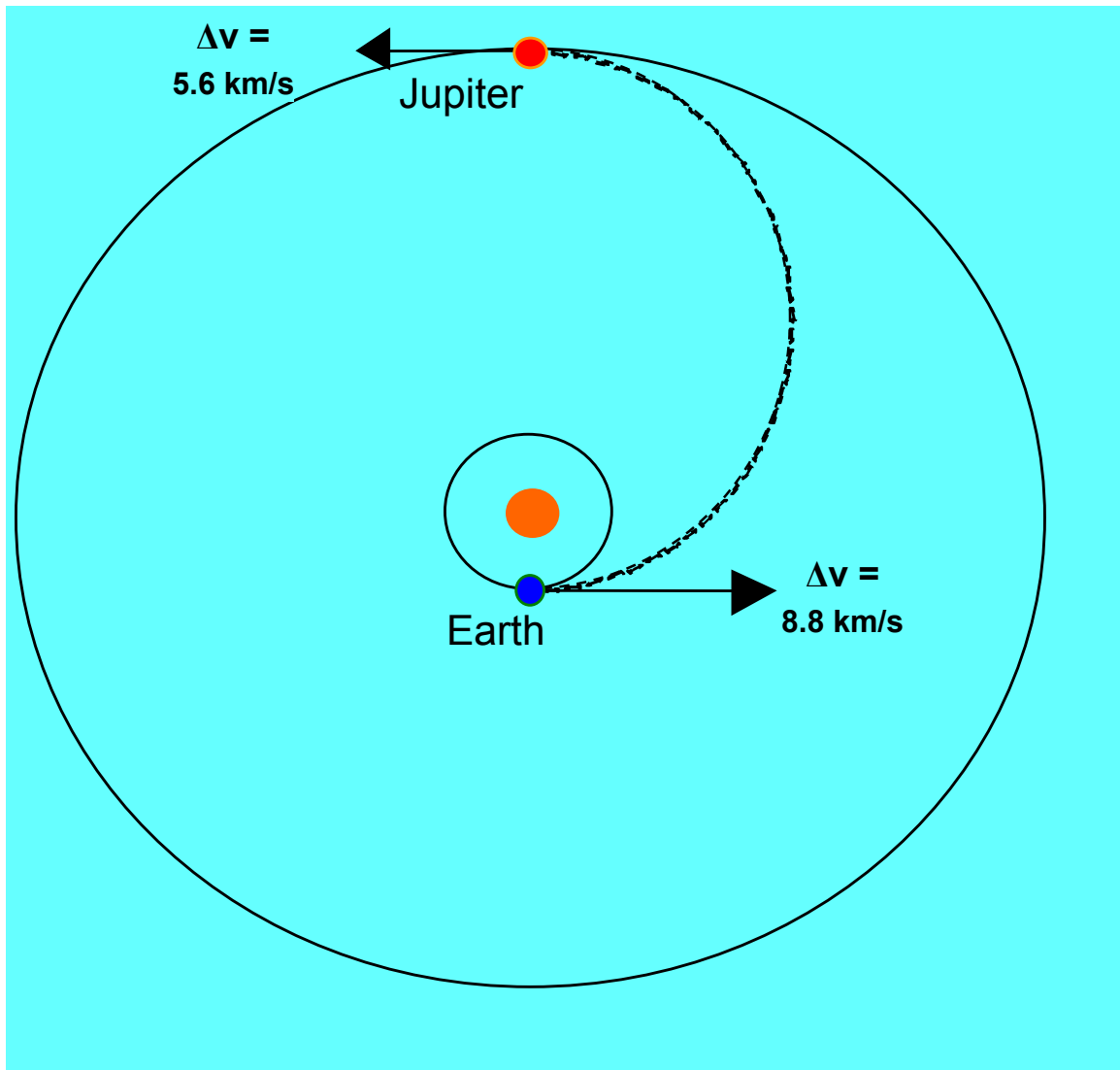


# Escape from Planetary “Surfaces” Can Be Difficult

<i>Planet</i>	<i>Surface escape <math>\Delta v</math> (km/s)</i>	<i>Sun escape <math>\Delta v</math> (km/s)</i>
Mercury	4.25	67.7
Venus	10.4	49.6
Earth	11.2	42.1
Mars	5.03	34.1
Jupiter	59.6	18.5
Saturn	35.5	13.7
Uranus	21.4	9.62
Neptune	23.8	7.69
Pluto	0.97	6.71



# Hohmann (Minimum-Energy) Two-Impulse Transfer





# Characteristics of Hohmann Transfers from Earth into the Solar System

<b><i>Planet</i></b>	<b><i>Total <math>\Delta v</math> (km/s)</i></b>	<b><i>Travel time (year)</i></b>
Mercury	-17.2	0.29
Venus	-5.27	0.40
Mars	5.56	0.71
Asteroid belt	11.7	1.4
Jupiter	14.4	2.7
Saturn	15.7	6.0
Uranus	15.9	16
Neptune	15.7	30
Pluto	15.5	45



# Hohmann Transfer $\Delta v$ Values

## Drop Slightly for Outermost Planets

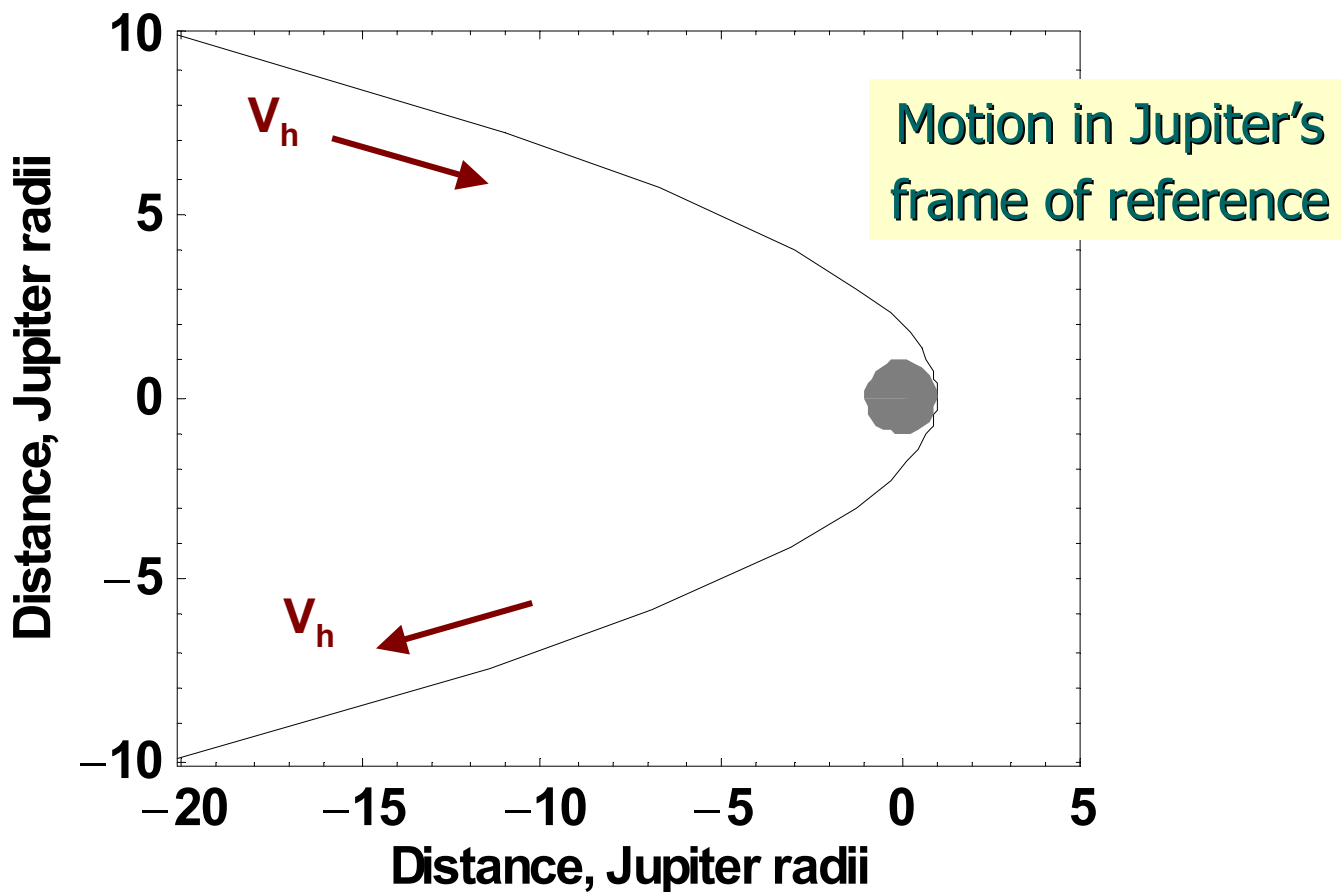
<b><i>Planet</i></b>	<b><i>First <math>\Delta v</math></i></b> <b><i>(km/s)</i></b>	<b><i>Second <math>\Delta v</math></i></b> <b><i>(km/s)</i></b>	<b><i>Total <math>\Delta v</math></i></b> <b><i>(km/s)</i></b>
Saturn	10.30	5.44	15.7
Uranus	11.30	4.66	15.9
Neptune	11.60	4.05	15.7
Pluto	11.80	3.69	15.5



# How Can Main-Belt Asteroids Best Be Moved to Earth?

## Aim at Jupiter and Get a Gravity Assist!

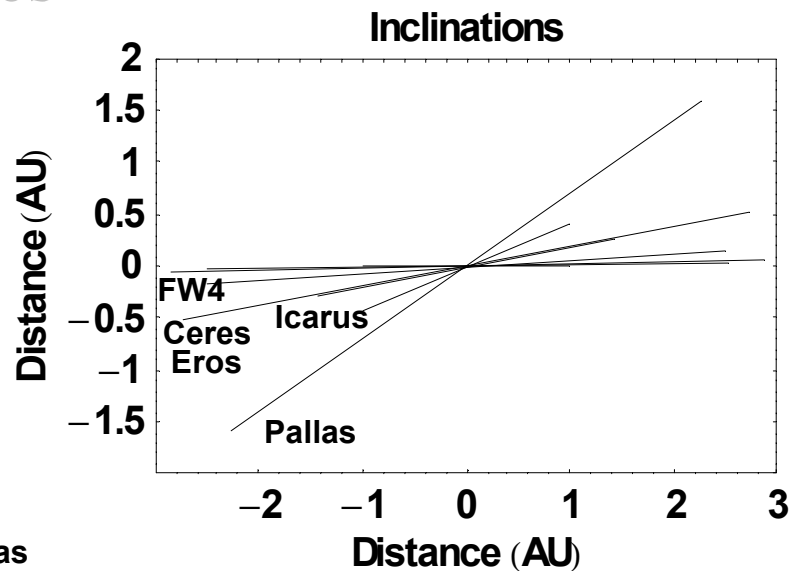
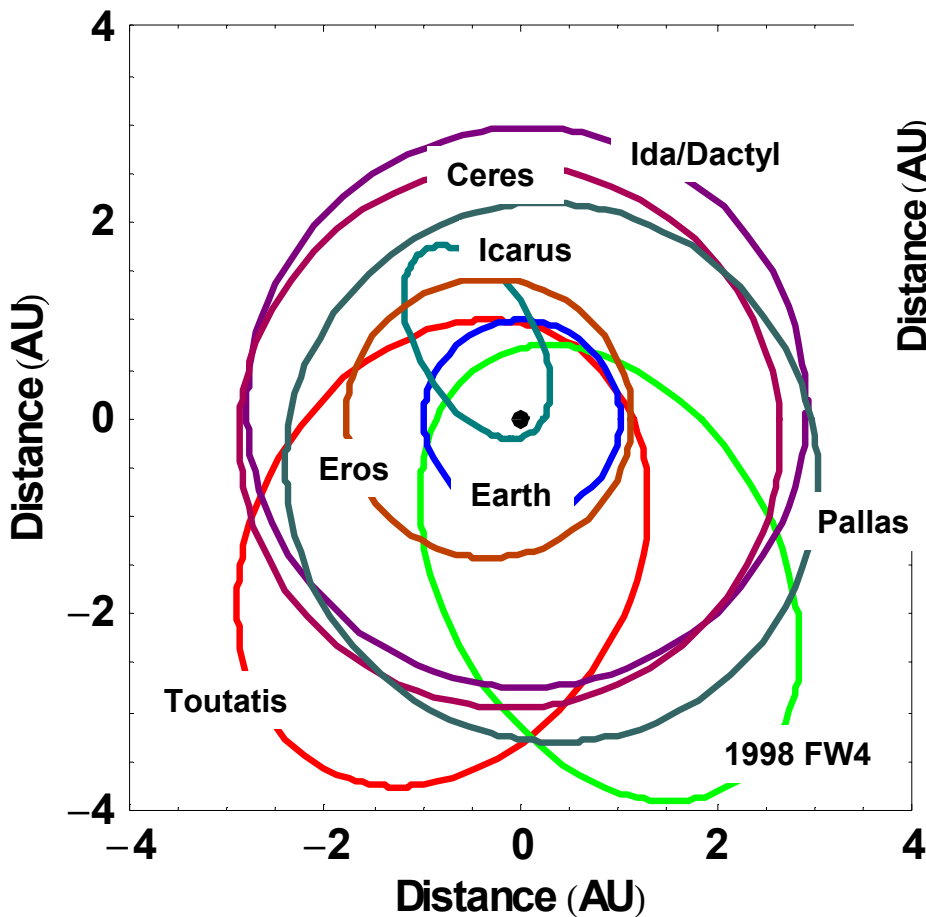
- In the spacecraft's frame of reference, the net result of the trade-off of momentum between it and Jupiter is a small change in the planet's velocity and a very large  $\Delta v$  ( $\sim 10$  km/s) for the spacecraft.





# Many Asteroids Exist Outside of the Main Belt

- Selected asteroid trajectories

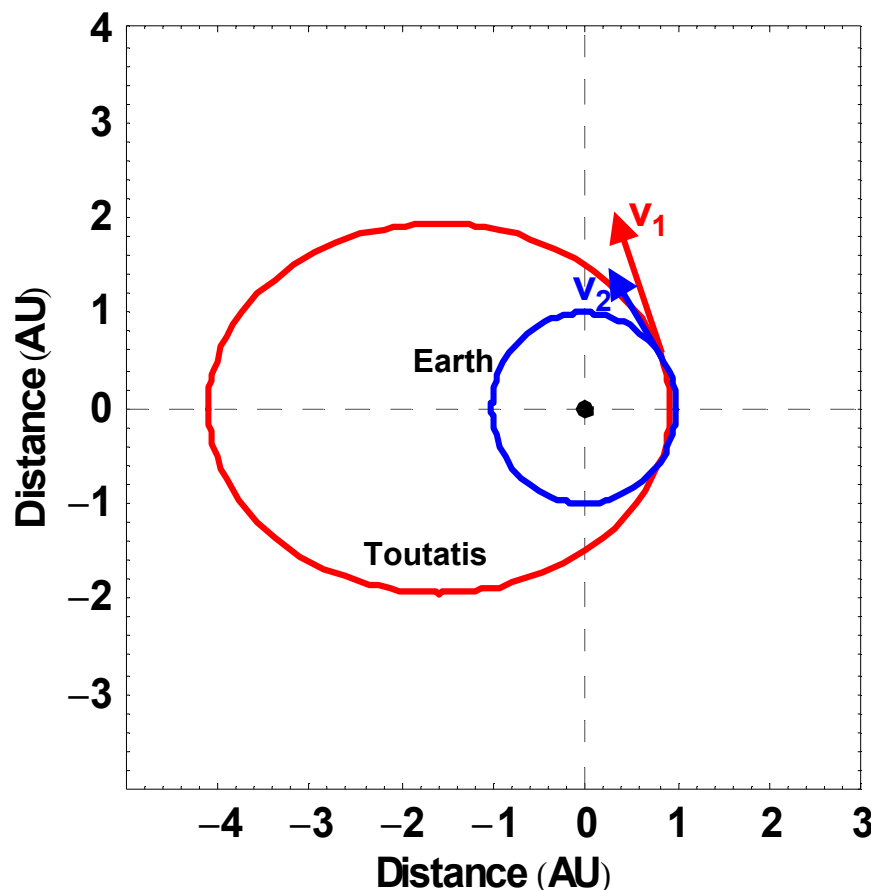






# Large Eccentricities Lead to Large $\Delta v$ 's for Single-Impulse Deflection of Asteroid Orbits

- Toutatis:  $a=2.51$  AU,  $e=0.63$ ,  $i=0.5^\circ$



- Velocity on an elliptic orbit is

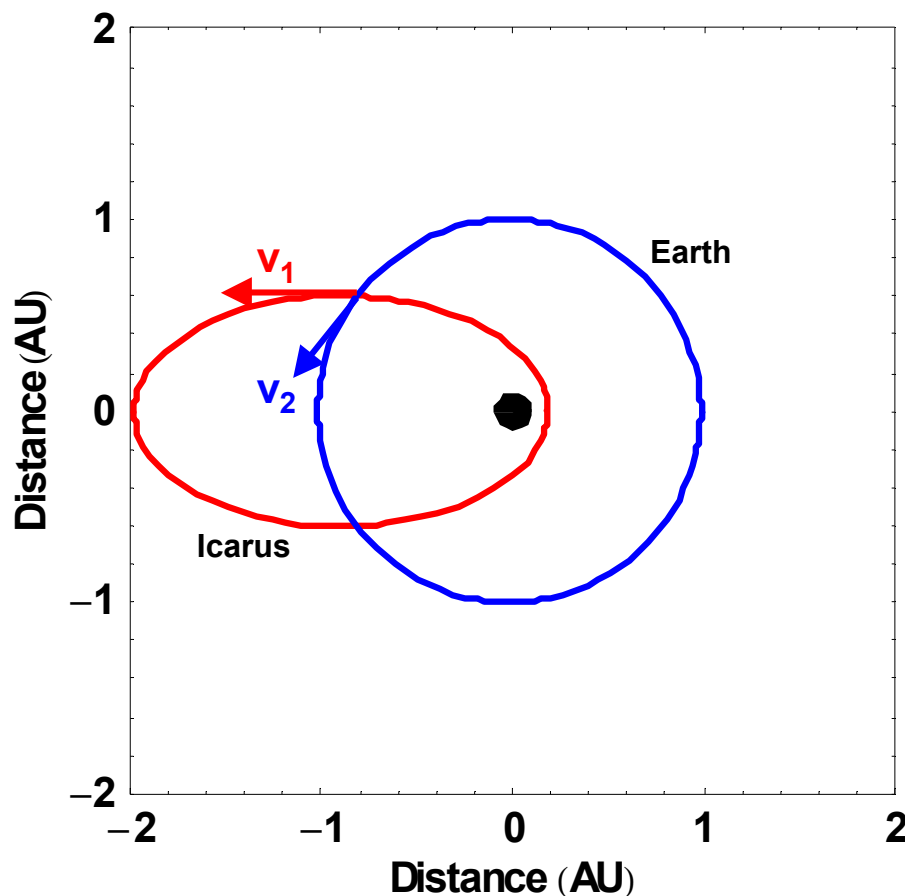
$$v = \left[ GM \left( \frac{2}{r} - \frac{1}{a} \right) \right]^{1/2}$$

- Velocity of Toutatis as it crosses Earth's orbit is  $v_1 = 37.7$  km/s.
- Earth's velocity is  $v_2 = 29.4$  km/s ( $e=0.017$  included).
- Angle between velocity vectors is  $38^\circ$ .
- Adding vectors gives  $\Delta v = 10.8$  km/s.



# Large Inclinations Substantially Increase $\Delta v$ 's for Single-Impulse Deflection of Asteroid Orbits

- Icarus:  $a=1.08$  AU,  $e=0.83$ ,  $i=22.9^\circ$



- Velocity of Icarus as it crosses Earth's orbit is  $v_1 = 30.5$  km/s.
- Earth's velocity is  $v_2=29.4$  km/s ( $e=0.017$  included).
- Angle between velocity vectors is  $60^\circ$ .
- Adding vectors *in plane* gives  $\Delta v=27.9$  km/s.
- Inclination of orbits adds another 23.2 km/s
- Total  $\Delta v=51$  km/s.



# Hohmann Trajectories Can Give Low $\Delta v$ 's for Some Asteroids

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- For asteroids with nearly circular orbits of low eccentricity and inclination,  $\Delta v$ 's can be  $< 2$  km/s.
  - For example, 1999 FA (~330 m diameter) has  $a=1.078$ ,  $e=0.133$ ,  $i=12$ .
    - The corresponding Hohmann trajectory to Earth has  $\Delta v=1.8$  km/s.
  - Some asteroid resource literature quotes  $\Delta v$ 's of 100's of m/s, but I have not personally verified these values.
- Note: the Moon can gravity assist with  $\sim 1$  km/s.