

Effect of Porosity

Purposely put porosity into UO₂

- *Good - Reduces gross swelling*
- *Bad - Reduces thermal conductivity*

Define;

$$P = \frac{\text{Volume of Pores}}{\text{Volume of Pores} + \text{Volume of Solid}}$$

Model of Heat Conductivity

(Figure 10.15)

Fraction of xsection area occupied by pore

$$k = P_C k(\text{Pore Tube}) + (1 - P_C) k_S$$

Fraction length occupied by pore tube

$$\frac{1}{k_{(\text{poretube})}} = \frac{P_L}{k_p} + \frac{1 - P_L}{k_S}$$

This produces ;

$$k = k_S (1 - P^{2/3}) \quad \text{where } P = P_C P_L$$

Radiation Transport (see figure 10.16)

$$k_p = k_g + 4 l_y T^3$$

thermal conductivity of gas

Empirical (to account for the minimum)

$$k = (3.11 + 0.0272 T)^{-1} + 5.39 \times 10^{-13} T^3$$

10.4 Temperature Profiles in Cylindrical Fuel Rods

$$T - T_s = \frac{HR^2}{4k} \left(1 - \frac{r^2}{R^2} \right)$$

both a function of r , t

Previously we may have used ,

$$\frac{(T - T_s)}{(T_0 - T_s)} = 1 - \frac{r^2}{R^2}$$

but this is not good enough when H and k are varying

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10.4.1 Volumetric Heating Rates

$$P = \frac{\text{Power}}{\text{Unit Length of Rod}} \quad \left(\frac{\text{W}}{\text{cm}} \right)$$

This is called the thermal rating

H Can Vary for at least 4 Reasons

Not normal 1.) Gradient in initial enrichment

Fast reactors 2.) Pu migration

Both LWR & FBR 3.) Burnout or breeding effects

Thermal reactors 4.) Flux effects

$$\frac{P}{(R_o^2 - r_o^2)} = \frac{2}{(R_o^2 - r_o^2)} \cdot \int_{r_o}^R rH(r)dr = \bar{H}$$

10.4.2

Thermal Conductivity Integral

integrating,

$$\frac{1}{r} \frac{d}{dr} rk \frac{dT}{dr} + H = 0 \quad \text{if H is constant}$$

first time,

$$rk \frac{dT}{dr} = -\frac{Hr^2}{2} \quad \text{(solid rod)}$$

again,

(conductivity integral)

$$\int_{T_s}^{T_o} kdT = \frac{HR^2}{4} = \frac{P}{4}$$

Major use of conductivity integral is that when T_s and P are known, it can be used to estimate T_0

$$\int_{T_s}^{T_0} k dT = \int_0^{T_0} k dT - \int_0^{T_s} k dT = \frac{P}{4}$$

This integral has been measured for a mixed oxide fuel

(See figure)

Value for T_m

$$= \int_0^{T_m} k dT = 93 \pm 4 \frac{W}{cm}$$

If we know T_s , P (from experimental measurements), then we can get a value of,

$$\int_0^{T_0} k dT$$

which in turn will give T_0 from figure 10.20

example; It is shown that as a result of self shielding, the heat generation rate in a thermal reactor fuel pin is ,

is reciprocal of neutron diffusion length

$$= \frac{1}{L} \frac{\sqrt{6}}{\sqrt{\bar{r}^2}}$$

\bar{r}^2 = mean Vector distance that a monoenergetic neutron travels from its source to where it is absorbed

$$H(r) = \frac{P}{R^2} \frac{(R)}{2I_1(R)} I_0(R)$$

Bessel Functions

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Using H(r) in equation above

$$k_{eff} = \frac{T_0}{T_s} = \frac{P}{4} \frac{I_0(R) - 1}{\frac{R}{2} \cdot I_1(R)}$$

See figure 10.21.

Note that reduced Conductivity Integral means lower T_0 , ---same as moving the heat source to the outside

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- Note flux depression in fast reactors is absent**

10.4.3

Effect of Fuel Restructuring

4 Main Regions -(Figure 10.23)

	Radius	T °C	$\frac{i}{s}, \%$
1.) Central Void	r₀	2800	0
2.) Columnar Region	r₀ to r₁	1700-2200	98-99
3.) Equiaxed Grains	r₁ to r₂	1600-1700	95-97
4.) As Fabricated	r₂ to r₃	1000	as fab.

Can determine the central void radius by;

$$r_0^2 = \frac{(1 - 2)}{1} r_1^2 + \frac{(2 - 3)}{1} r_2^2 \quad (10.70)$$

Note ; we have to correct volumetric heating rates by density differences

$$H_3 = \frac{\quad}{R^2} , \quad H_2 = \frac{\quad}{R^2} \cdot \frac{2}{3} , \dots\dots\dots$$

Using these values with the heat conduction eq., we find that things can be expressed as a function of as fabricated porosity

As fabricated region;

$$\frac{T_2}{T_s} k_3 dT = \frac{1}{4} \left(1 - \frac{r_2^2}{R^2} \right) \quad \mathbf{10.88}$$

Equiaxed Region; (10.89)

$$\frac{T_1}{T_2} k_2 dT = \frac{1}{4} \left(\frac{2}{3} \frac{r_2^2}{R^2} \left(1 - \frac{r_1^2}{r_2^2} \right) - \frac{3}{2} \ln \frac{r_2}{r_1} \right)$$

Columnar Region (10.90)

$$\frac{T_0}{T_1} k_1 dT = \frac{1}{4} \left(\frac{1}{3} \frac{r_1^2}{R^2} \left(1 - \frac{r_0^2}{r_1^2} \right) - \frac{r_0^2}{r_1^2} \ln \frac{r_1}{r_0} \right)$$

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Procedure to Find Temperature Distribution**

$T_s, \frac{3}{s} \text{-----} > T_1, \frac{1}{s} \text{-----} > \mathbf{Determine}$

$\text{known} \quad T_2, \frac{2}{s} \quad \text{-----} \quad T_{i-1} \quad \text{-----} \quad T_i \quad \text{-----} \quad k_i dT$

**Experiment
i.e., for 95% dense material (10.91)**

$$k_i dT = \int_{T_i}^{T_{i-1}} k dT - \int_{T_i}^{T_{i-1}} k dT \cdot \frac{f(P_i)}{f(0.05)}$$

where $f(P_i)$ = reduction in thermal conductivity
in the i th zone with P_i porosity
(see eq. 10.40, 10.42, 10.44)

once $k_i dT$ is determined for as fabricated and
equiaxed zones by eq. 10.91;

then eq. 10.88 is used to find $\frac{r_2}{R}$

then eq. 10.89 is used to find $\frac{r_1}{R}$

then eq. 10.70 is used to find r_0
 T_0

then eq. 10.90 is used to find $k_1 dT$

T_1
 T_0

then eq. 10.91 is used to find $k dT$

0

P

then fig. 10.20 gives T_0 (fig. 10.24)

10.4.4 Fuel Surface Temperature

So far we have assumed we know T_s , but T_s is a function of axial position (z)

From heat transfer considerations;

changes with z

$$T_s = T_{coolant} + \frac{P}{2 R_c U}$$

$$T_{inlet} + \frac{\#rods}{QC_{pc}} \int_0^z (z') dz' \frac{1}{U} = \frac{1}{h_{gap}} + \frac{t_c}{k_c} + \frac{1}{h_{coolant}}$$

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Table 10.5 - Note Importance of Gap

10.4.5 Conductance of Fuel Cladding -Gap

<u>Initial Conditions</u>	<u>End of life</u>
<i>gap thickness</i> 100 μm	0 to few μm
<i>gap gas.....He</i>	He + Kr+ Xe
<i>gas pressure</i> 1bar	50-100 bar

Conductance of open gap

$$h_{gap} = \frac{k_g}{t_{gap}} + \frac{4 T^3}{\frac{1}{c} + \frac{1}{f} - 1}$$

Thermal Conductivity of Gases

$$k_g \text{ (pure gas)} = A \times 10^{-6} T^{0.79} \quad \text{W/cm}^\circ\text{C}$$

15.8 He

1.15 Kr

0.72 Xe

Thermal Conductivity of Gas Mixture

$$k_g = (k_{He})^{x_{He}} (k_{Xe})^{1-x_{He}}$$

At normally small gaps during operation, the gas conduction term dominates

Closed Gap

When fuel expands to contact the cladding, the heat transfer is across the various contact points and the gas in between

$$h_{\text{gap}} = \frac{k_g}{(g_c + g_f)} + C \frac{2k_f k_c}{k_f + k_c} \frac{P_i}{\frac{1}{2}H}$$

$$h_{\text{gap}} = \frac{1\text{Watt}}{\text{cm}^2 \text{ } ^\circ\text{C}}$$